PHBS WORKING PAPER SERIES

Turbulent Business Cycles

Ding Dong
Hong Kong University of Science and Technology

Zheng Liu
Federal Reserve Bank of San Francisco

Pengfei Wang
Peking University

Abstract

Recessions are associated with sharp increases in turbulence that reshuffle firms' productivity rankings. To study the business cycle implications of turbulence shocks, we use Compustat data to construct a measure of turbulence based on the (inverse of) Spearman correlations of firms' productivity rankings between adjacent years. We document evidence that turbulence rises in recessions, reallocating labor and capital from high- to low-productivity firms and reducing aggregate TFP and the stock market value of firms. A real business cycle model with heterogeneous firms and financial frictions can generate the observed macroeconomic and reallocation effects of turbulence. In the model, increased turbulence makes high-productivity firms less likely to remain productive, reducing their expected equity values and tightening their borrowing constraints relative to low-productivity firms. This leads to a reallocation that reduces aggregate TFP. Unlike uncertainty, turbulence changes both the conditional mean and the conditional variance of the firm productivity distribution, enabling a turbulence shock to generate a recession with synchronized declines in aggregate activities.

Peking University HSBC Business School University
Town, Nanshan District Shenzhen 518055, China

PHBS
北京大学汇丰商学院

TURBULENT BUSINESS CYCLES

DING DONG, ZHENG LIU, AND PENGFEI WANG

ABSTRACT. Recessions are associated with sharp increases in turbulence that reshuffle firms' productivity rankings. To study the business cycle implications of turbulence shocks, we use Compustat data to construct a measure of turbulence based on the (inverse of) Spearman correlations of firms' productivity rankings between adjacent years. We document evidence that turbulence rises in recessions, reallocating labor and capital from high- to low-productivity firms and reducing aggregate TFP and the stock market value of firms. A real business cycle model with heterogeneous firms and financial frictions can generate the observed macroeconomic and reallocation effects of turbulence. In the model, increased turbulence makes high-productivity firms less likely to remain productive, reducing their expected equity values and tightening their borrowing constraints relative to low-productivity firms. This leads to a reallocation that reduces aggregate TFP. Unlike uncertainty, turbulence changes both the conditional mean and the conditional variance of the firm productivity distribution, enabling a turbulence shock to generate a recession with synchronized declines in aggregate activities.

I. INTRODUCTION

Recessions are characterized by declines in aggregate economic activity. They are also characterized by a sharp rise in micro-level turbulence with increased churning of firms' productivity rankings. This paper studies the macroeconomic and reallocation effects of turbulence shocks over business cycles.

We develop an empirical measure of turbulence using data from publicly traded U.S. firms listed in Compustat. We first construct a measure of firm-level total factor productivity (TFP) following the approach in the literature (Syverson, 2004; Foster et al., 2008; Bloom et al., 2018). We then sort the firm-level TFP in each year and estimate the Spearman rank correlations (denoted by ρ_t) between adjacent years. A low Spearman correlation indicates more churning of firm rankings in the productivity distribution: a high-productivity firm this year is less likely to maintain its productivity ranking next year; whereas a low-productivity firm now might become more productive in the future. Turbulence is inversely related to the Spearman correlation of firm-level TFP, and we measure it by $1 - \rho_t$.

Our measure of turbulence is countercyclical, rising sharply in recessions. We present firm-level evidence that an increase in turbulence reallocates labor and capital from high- to low-productivity firms, with the magnitude of the reallocation effects depending partly on financial frictions. Reflecting its reallocation effects, turbulence is negatively correlated with aggregate manufacturing TFP and the stock market value of firms. Turbulence is also associated with synchronized and persistent declines in real GDP, consumption, investment, and employment.

To understand the economic mechanism through which turbulence can drive macroeconomic fluctuations and cross-sectional reallocation, we construct a real business cycle (RBC) model with heterogeneous firms and financial frictions. In the model, firms produce a homogeneous good using capital and labor, subject to idiosyncratic productivity shocks. Firms rely on external financing of working capital, with the borrowing capacity constrained by a fraction of the expected future equity value (Jermann and Quadrini, 2012; Liu and Wang, 2014; Lian and Ma, 2021). Firms also face idiosyncratic production distortions, reflecting differential policy interventions or government subsidies at the firm level (Hsieh and Klenow, 2009; Buera and Shin, 2013; Moll, 2014). At each given level of productivity, firms with sufficiently high levels of subsidies choose to operate, facing binding credit constraints. Those with low levels of subsidies remain inactive. There is an endogenously determined threshold level of subsidy, at which a firm is indifferent between producing and staying inactive.

Under the stochastic process of the idiosyncratic productivity shocks, a firm can maintain its productivity from the current period to the next period with a time-varying probability ρ_t. With the complementary probability $1-\rho_t$, the firm's productivity will be an independent and identically distributed (i.i.d.) random variable. As we have alluded to, a lower value of ρ_t implies more frequent switching in firm productivity rankings between adjacent periods or, equivalently, greater turbulence.

The model predicts that a shock that increases turbulence leads to a recession. With greater turbulence, a high-productivity firm today would be less likely to remain productive

in the future and a low-productivity firm today would be more likely to get a better productivity draw in the future. Thus, the expected equity value of a high-productivity firm falls relative to that of a low-productivity firm. Since firms' borrowing capacity depends on the expected equity value, turbulence tightens the current-period credit constraints for high-productivity firms disproportionately and reallocates labor and capital from high- to low-productivity firms. This reallocation reduces aggregate TFP. The endogenous decline in TFP is quantitively important, enabling the model to generate a recession with synchronized declines in aggregate output, consumption, investment, and labor hours. These model predictions are in line with empirical evidence.

Financial frictions are crucial for amplifying the macroeconomic effects of turbulence shocks. Since labor and capital are perfectly mobile across firms, competition for input factors from high-productivity firms bids up wages and capital rents. Absent credit constraints and production subsidies, resources would be concentrated in the most productive firms, and the equilibrium allocation would be efficient. Credit constraints and idiosyncratic production distortions allow a fraction of firms at each level of productivity to stay active in production. Such financial frictions lead to steady-state misallocation; they also create room for turbulence shocks to generate reallocation across firms with different productivity levels.

The presence of financial frictions implies that competitive equilibrium allocations are inefficient. Appropriate policy interventions can potentially mitigate credit constraints and improve allocative efficiency. Since financial frictions are the key transmission channel for turbulence, policy interventions that alleviate credit constraints might mitigate its recessionary effect.

We use our model framework to evaluate the effectiveness of two alternative policy interventions for stabilizing turbulence-driven recessions. The first policy is a borrowing subsidy that reduces the effective costs of hiring capital and labor, therefore reducing the amount of working capital that firms need to finance. The second policy is credit easing, under which the government injects liquidity to enhance the borrowing capacity of active firms. Each policy is transitory and unexpected, and it is triggered by the realization of a turbulence shock, with the same persistence as that of the shock.

Under our calibration, both types of policies are effective for mitigating the recessionary effects of turbulence relative to the *laissez-faire* benchmark economy with no policy interventions. However, the policies operate through different channels and therefore have different implications for reallocation.

Borrowing subsidies reduce the effective costs of hiring input factors for all firms, expanding the set of active firms at each level of productivity and boosting aggregate output. However,

by enabling a larger fraction of low-productivity firms to stay active, the policy exacerbates misallocation, reducing aggregate TFP relative to the benchmark. The decline in TFP partly offsets the stimulus effects on aggregate output.

Credit easing expands the borrowing capacity for active firms. Competition for input factors from high-productivity firms pushes up equilibrium wages and capital rents, forcing some low-productivity firms to stay inactive. This reallocation improves aggregate TFP, contributing to increased output.[1]

II. Related literature

Our work is closely related to the important contribution of Bloom et al. (2018), who study the macroeconomic implications of micro-level uncertainty. They show that, in a real business cycle model with capital and labor adjustment costs, an increase in micro-level uncertainty (i.e., an increase in the standard deviation of the firm-level TFP shocks) reduces net aggregate investment, net hiring, and aggregate output. However, in their model, aggregate consumption rises following an uncertainty shock. Generating a recession with aggregate comovements requires a simultaneous negative shock to the level of aggregate TFP.

Unlike uncertainty, turbulence changes not just the conditional variance but also the conditional mean of firm-level productivity. Following an increase in turbulence, firms with high productivity in the current period may not be as productive in the future. Working through financial frictions, the turbulence-induced changes in conditional expectations of future firm-level productivity lead to reallocation from high- to low-productivity firms, reducing aggregate TFP. The reduction in TFP in turn leads to a recession with aggregate comovements.

Our model illustrates the importance of financial frictions for propagating turbulence shocks.[2] Existing studies show that financial frictions are also important for the transmission of uncertainty shocks (Gilchrist et al., 2014; Christiano et al., 2014; Alfaro et al., 2018;

---

[1]The two types of policy interventions—borrowing subsidies and credit easing—do not necessarily improve welfare relative to the benchmark, because they both incur a deadweight loss. We use these counterfactual policies to highlight the transmission mechanism of turbulence shocks. We do not study optimal policy here because welfare depends on the calibration of the sizes of the deadweight losses (Gertler and Karadi, 2011).

[2]The global financial crisis of 2008-2009 has spurred a large literature that incorporates financial frictions into business cycle models, building on the seminal contributions of Bernanke et al. (1999) and Kiyotaki and Moore (1997). Examples include Jermann and Quadrini (2012), Gertler et al. (2012), Liu et al. (2013), Christiano et al. (2014), Gertler and Kiyotaki (2015), and Lian and Ma (2021). For recent surveys of this literature, see Christiano et al. (2018) and Gertler and Gilchrist (2018).

Arellano et al., 2019).[3] In the model of Arellano et al. (2019), for example, hiring is risky because firms need to finance input costs before they receive revenues, and firms face idiosyncratic productivity shocks between paying for inputs and receiving revenues. An increase in the volatility of idiosyncratic shocks raises default risks, and firms respond by pulling back hiring and reducing production. Since firms are ex ante identical, they make identical hiring decisions. Thus, an increase in uncertainty in their model (i.e., firm-level volatility) does not lead to reallocation of capital and labor inputs. In our model, however, reallocation is the central mechanism for propagating turbulence shocks.

Our work is related to the economic development literature on capital misallocation under financial frictions (Midrigan and Xu, 2014; Moll, 2014; Buera and Shin, 2013; Liu et al., 2021). Indeed, our measure of turbulence is similar to the persistence of idiosyncratic productivity in the continuous-time model of Moll (2014) and Dou et al. (2021). More persistent productivity shocks imply relatively smaller steady-state productivity losses but also slower transitions to the steady-state (Moll, 2014). Other things being equal, the less persistent the idiosyncratic productivity shocks are, the greater the impact of financial frictions on aggregate productivity (Buera and Shin, 2013). We focus on the business cycle implications of turbulence. Thus, our work complements this development literature.

The countercyclical behavior of turbulence that we find is consistent with other empirical studies based on different data and measurements. For example, Aghion et al. (2021) construct a measure of turbulence based on the rate of new product additions and subtractions (i.e., product churn) using US Census of Manufactures data. They find that product churn rises sharply during recessions. Bernard and Okubo (2016) also report evidence of countercyclical product churn based on Japanese manufacturing data. We add to this empirical literature by documenting the macroeconomic and reallocation effects of turbulence.[4]

To our knowledge, our paper represents a first attempt to study the transmission mechanism of turbulence shocks over the business cycle using firm-level data and a quantitative business cycle model featuring firm heterogeneity and financial frictions.

---

[3]There is a large strand of literature on the macroeconomic effects of uncertainty shocks. Examples include Bloom (2009), Bachmann et al. (2013), Fernández-Villaverde et al. (2015), Jurado et al. (2015), Baker et al. (2016), Leduc and Liu (2016), Basu and Bundick (2017), Bansal et al. (2019), Berger et al. (2020), and many others. For recent surveys of the uncertainty literature, see Bloom (2014) and Fernández-Villaverde and Guerrón-Quintana (2020).

[4]Similar reallocation effects can arise from labor market churns (Pratap and Quintin, 2011) or supply-chain disruptions (Meier, 2020).

III. Measuring micro-level turbulence and its macroeconomic effects

This section describes our empirical methods for measuring micro-level turbulence and documents some stylized facts about the macroeconomic effects of turbulence.

III.1. **Empirical methodology.** Consider the production function for firm j in period t

$$Y_{jt} = z_{jt}F(K_{jt}, N_{jt}), \tag{1}$$

where Y_{jt} denotes value-added output, K_{jt} and N_{jt} denote capital and labor inputs, respectively, and $F(K, N)$ is the production function. The term z_{jt} denotes firm j's TFP that follows the stochastic process

$$z_{j,t+1} = \begin{cases} z_{jt} & \text{with prob} \quad \rho_t, \\ \tilde{z} & \text{with prob} \quad 1 - \rho_t, \end{cases} \tag{2}$$

where $\tilde{z}$ is an i.i.d. random variable with the cumulative density function $\tilde{G}(z)$.

The term ρ_t measures the persistence of firm-level TFP. In the extreme case with $\rho_t = 1$ for all t, a firm's productivity level would be permanent: high-productivity firms would remain productive and low-productivity firms would remain unproductive. In the other extreme with $\rho_t = 0$, firm productivity would be an i.i.d. process, with no persistence. In the more general case with $\rho_t \in (0, 1)$, firm productivity is persistent, and the persistence is time varying. A decline in ρ_t implies that high-productivity firms in period t would be less likely to remain productive in period $t + 1$ and low-productivity firms in period t would have a chance to draw a high productivity in period $t+1$. Thus a decline in ρ_t increases the churn of firm rankings in the productivity distribution. We measure micro-level turbulence by $1 - \rho_t$.

Turbulence is related to but different from the micro-level uncertainty studied by Bloom et al. (2018). An increase in micro-level uncertainty corresponds to a mean-preserving spread of the cross-sectional productivity distribution—an increase in the variance or inter-quartile range (IQR) of productivity. An increase in turbulence also raises the conditional variance of the productivity distribution, as does uncertainty. Thus, turbulence is positively correlated with micro-level uncertainty.[5] However, unlike uncertainty, turbulence does not affect the *ex ante* stationary distribution of productivity—it is an *ex ante* distribution-preserving shock, as we show in Proposition 1 below.[6]

---

[5] For example, the correlation between our turbulence measure and the IQR of firm-level TFP from Compustat data is about 0.55.

[6] The distribution-preserving turbulence that we study here can be viewed a discrete-time counterpart to the persistence of idiosyncratic productivity shocks in the continuous-time models of Moll (2014) and Dou et al. (2021), which is also orthogonal to the stationary productivity distribution.

TABLE 1. Summary statistics of our samples with publicly traded manufacturing firms

	Sample 1			Sample 2		
Variable	Mean	SD	N	Mean	SD	N
Log Asset (1m)	4.7	2.7	75409	5.8	2.7	23847
Log Value-Added (1m)	3.9	2.8	71645	5.1	2.7	23514
Log Capital (1m)	2.8	3.1	74132	4.1	3.0	23716
Log Market Value	5.0	2.6	69923	5.9	2.6	23283
No. of Workers (1000)	6.8	25.2	75518	12.8	32.0	23849
Employment Growth (%)	3.9	38.7	67311	3.1	26.5	22845
Capital Growth (%)	6.7	57.2	66557	5.5	39.9	22762
Sales Growth (%)	8.9	60.0	64171	6.9	39.0	22518
Market-Value Growth(%)	0.4	77.7	62841	6.8	57.6	22334

Note: Sample 1 covers all listed firms in all manufacturing industries (NAICS code 31 to 33). Sample 2 covers the firms with 25+ years of observations in all manufacturing industries.

Source: Compustat, NBER-CES, and authors' calculations.

Proposition 1. The cross-sectional stationary distribution of idiosyncratic productivity (denoted by $G_t(z)$) is invariant to the realization of ρ_t.

Proof. Under the stochastic process of idiosyncratic productivity specified in Eq. (2), the cumulative density function of productivity is given by

$$
\begin{aligned}
G_{t+1}(z) &= Pr(z_{t+1} \leq z) \\
&= Pr(z_t \leq z)\rho_t + Pr(\tilde{z} \leq z)(1 - \rho_t) \\
&= G_t(z)\rho_t + \tilde{G}(z)(1 - \rho_t).
\end{aligned}
\tag{3}
$$

Under the stationarity of the distribution of z, we have $G_t(z) = \tilde{G}(z)$ for all t. Thus, the stationary distribution is independent of the realization of ρ_t. $\square$

III.1.1. *Data.* We use firm-level data from Compustat Fundamentals Annual database. To obtain measures of industry-level employment, payroll, and price indices, we use information

from the NBER-CES Manufacturing Industry Database.[7] By combining these two data sources, we obtain an unbalanced panel with 75,518 firm-year observations. This full sample (Sample 1) includes all listed firms in all manufacturing industries covered by NBER-CES in the years from 1958 to 2016.[8] Table 1 presents the summary statistics of our samples.

Following Bloom et al. (2018), we focus on the subset of firms with 25+ years of observations in our sample. We use this pseudo-balanced panel as our baseline sample (Sample 2) for estimating firm-level TFP. The baseline sample contains about 23,000 firm-year observations. Since firms in the baseline sample are older than those in the full sample, they are also larger on average in terms of assets, value added, capital, and employment, although their average growth rates of employment and capital are slower.[9]

III.1.2. *Measuring turbulence.* We construct a measure of micro-level turbulence based on firm-level TFP.

Following the approach in the literature (Syverson, 2004; Foster et al., 2008; Bloom et al., 2018), we measure firm-level TFP based on the Solow residual calculated from the production function

$$tfp_{ijt} = y_{ijt} - \alpha_{it}k_{ijt} - (1 - \alpha_{it})n_{ijt}, \tag{4}$$

where tfp_{ijt} denotes the TFP (in log units) of firm j in industry i and year t, and y_{ijt}, k_{ijt} and n_{ijt} denote the firm's value added, capital input, and labor input, respectively, all in log units. Following Bloom et al. (2018), we assume that the cost share of capital input α_{it} is common for all firms within an industry i, although it can vary across time.[10]

---

[7]The Compustat database is accessed through Wharton Research Data Service at: https://wrds-web.wharton.upenn.edu/wrds/. The NBER-CES database is accessed through https://www.nber.org/research/data/nber-ces-manufacturing-industry-database.

[8]We include firms incorporated in the US (Compustat fic='USA') that trade on major stock exchanges (NYSE, AMEX, and NASDAQ, Compustat exchg = 11, 12 or 14), for which the native currency is US dollars (Compustat curcd='USD'). We exclude firm-year observations with obvious errors: missing or nonpositive values in reported revenue, employment, and capital. We remove a firm if it was involved in a major merger or acquisition that affected its asset by more than 10 percent.

[9]In a robustness check, we further narrow down the sample and focus on industries with more than 20 firms in each year. This sample (Sample 3) contains about 22,000 firm-year observations. Firms in Sample 3 have similar characteristics as those in Sample 2.

[10]In our sample, the average value of the cost share of capital (weighted by the value of shipment) is about 0.34. We provide some details of our approach to measuring value added, capital and labor inputs, and the capital share in Appendix A. Although our baseline measure of turbulence is constructed based on a production function with constant returns to scale in Eq. (4), the cyclical properties and the macroeconomic and reallocation effects of turbulence are similar when we construct an alternative measure of turbulence based on a production function with decreasing returns to scale (see Appendix B).
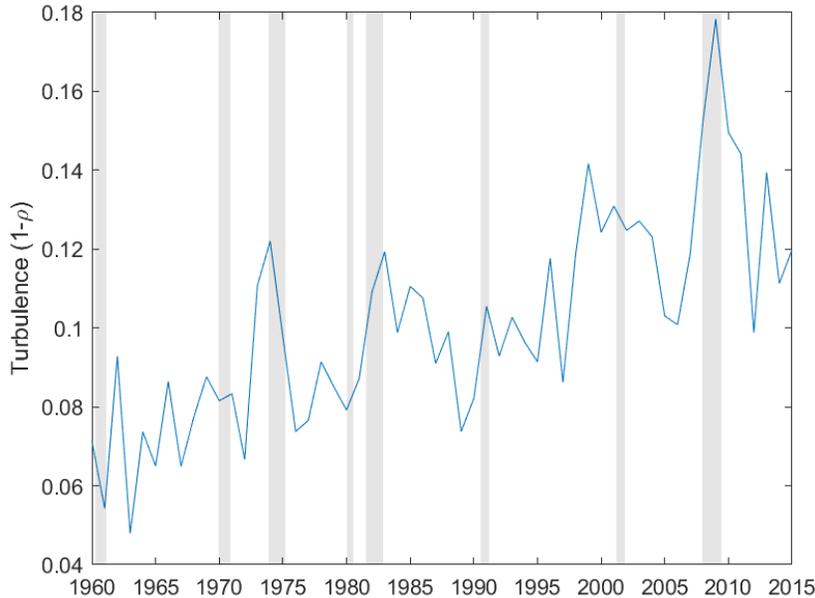
FIGURE 1. Measured micro-level turbulence

Note: Turbulence is measured by $1 - \rho_t$, where ρ_t is the Spearman correlation of firm TFP rankings between year t and year $t + 1$. The gray shaded bars indicate NBER recession dates.

Source: Compustat, NBER-CES, BLS, and authors' calculations.

After obtaining firm-level TFP, we construct a measure of turbulence following the approach of Bloom et al. (2018). Specifically, we rank firms within each industry (at the 3-digit level) by deciles of their productivity levels. We then compute the Spearman rank correlations of firm TFP between year t and year $t+1$. The time series of the Spearman correlations corresponds to our measure of ρ_t. Turbulence is measured by $1 - \rho_t$. Intuitively, a decline in ρ_t implies that a high-productivity firm in year t would be less likely to remain as productive in $t+1$, whereas a low-productivity firm in year t might get a high productivity draw in year $t + 1$. A reduction in ρ_t reshuffles productivity rankings across firms between t and $t + 1$, increasing turbulence.[11]

---

[11]Bloom et al. (2018) also estimate the Spearman correlation of plant rankings in the TFP distribution across adjacent years using Census Manufacturing (CM) data (see Figure A1 in their online appendix at `https://nbloom.people.stanford.edu/sites/g/files/sbiybj4746/f/rubc_appendix_0.pdf`). Despite the difference in the samples, our measure of ρ_t is highly correlated with theirs, with a correlation coefficient of 0.49.

III.1.3. *Cyclical properties of turbulence.* Figure 1 plots the time series of firm-level turbulence from 1960 to 2015. The mean, standard deviation, and autocorrelation of the estimated ρ_t are 0.90, 0.026, and 0.66, respectively. The figure shows that turbulence is countercyclical, rising sharply in recessions.[12]

Our measure of turbulence is negatively correlated with manufacturing TFP, as shown in panel A of figure 2. A rise in turbulence (blue line) is typically associated with a decline in TFP relative to trend (red line), and the correlation between the two series is about -0.28.

Turbulence is also negatively correlated with the stock market value of firms, as shown in panel B of figure 2. We consider two alternative measures of the firm value. One is the market value of assets ("asset value," red dashed line) calculated based on firms' stock prices at the end of the fiscal year, multiplied by the shares outstanding and deflated by the consumer price index. The other is the market value of equity ("equity value," red solid line) calculated based on market equity plus assets, net of book equity following Eisfeldt and Rampini (2006). The correlations between turbulence with the asset value and the equity value are both negative, at -0.35 and -0.43, respectively.[13]

III.2. **Reallocation effects of turbulence.** To examine the reallocation effects of turbulence, we estimate the empirical specification

$$x_{jt} = \beta_0 + \beta_1 High\_TFP_{jt} + \beta_2 Turb_t * High\_TFP_{jt} + \mu_j + \eta_t + \epsilon_{jt}, \tag{5}$$

where the dependent variable x_{jt} denotes the growth rate of employment, capital, sales, or market value of firm j in year t from $t-1$, $Turb_t$ denotes measured turbulence, and $High\_TFP_{jt}$ is a dummy variable that equals one if firm j's TFP level is above the median within its industry and zero otherwise. To mitigate potential biases associated with firm entries and exits, we focus on a pseudo balanced panel, with firms appearing at least 25 years in our sample from 1958 to 2016 (Sample 2), following Bloom et al. (2018). In estimating (5), we control for firm fixed effects (μ_j) and year fixed effects (η_t). The term ϵ_{jt} denotes regression errors.

The relative sensitivity of the firm-level activity of high-productivity firms to turbulence is captured by the coefficient on the interaction term (i.e., β_2). The parameter β_1 measures the

---

[12]In Appendix A, we show that the baseline estimate of ρ_t is robust to alternative samples and alternative approaches to measuring TFP. Our measured turbulence displays an upward trend. Since an increase in turbulence raises firm-level volatility, the trend increase in turbulence is consistent with the empirical evidence that the volatility for publicly traded firms has increased steadily over time, whereas the volatility of privately held firms has declined (Davis et al., 2006).

[13]In Compustat, the firm stock price at the end of the fiscal year is the variable "PRCC_F," the shares outstanding is "CSHO," the firm asset is "AT," and the book equity is "CEQ."
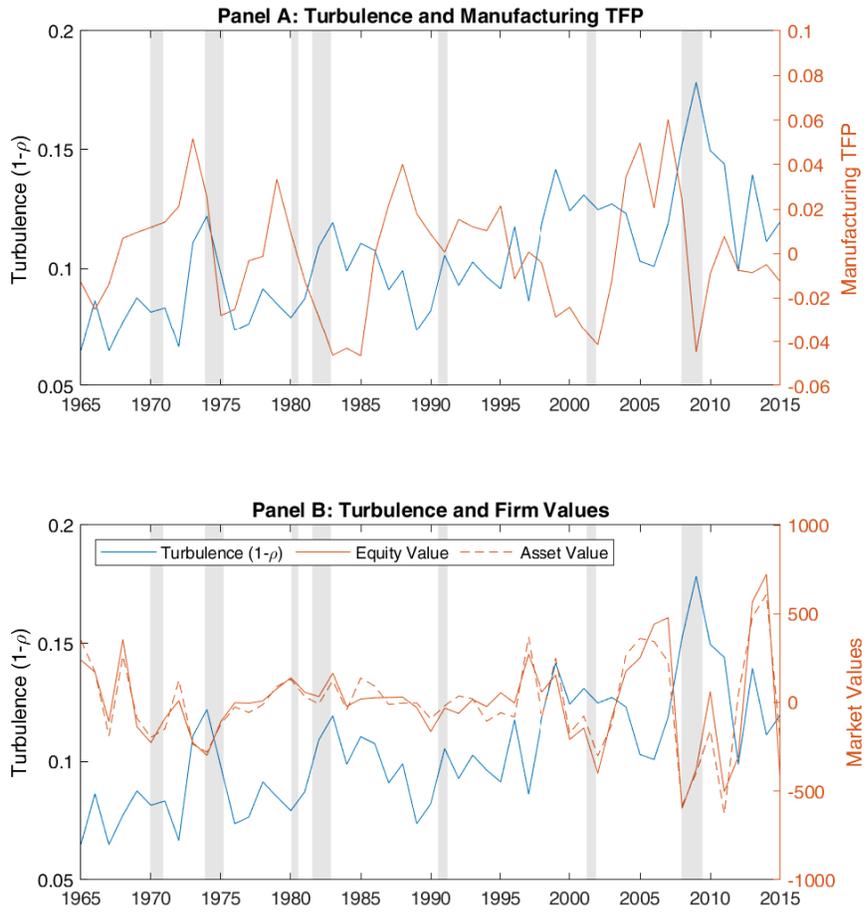
FIGURE 2. Correlation between Turbulence and TFP & Firm Values

Note: The series of manufacturing TFP is computed as an average of firm-level TFP in our benchmark sample, weighted by sales. The TFP index is detrended by the HP filter with a smoothing parameter of 100. The market value of assets and the market value of equity are both detrended by the HP filter with a smoothing parameter of 100. The gray shaded bars indicate NBER recession dates.

average effects of productivity on firm-level activity absent turbulence shocks. The parameter β_0 is a constant intercept. The estimation results are displayed in Table 2.

In the baseline regressions, the estimated values of β_2 are negative and statistically significant at the 99-percent confidence level for all measures of firm growth. Thus, an increase in turbulence is associated with declines in the firm-level growth rates for high-productivity

TABLE 2. Impact of turbulence on firms with different levels of productivity

Dep. Var.	Δn_{jt}	Δk_{jt}	Δy_{jt}	Δv_{jt}
	(1)	(2)	(3)	(4)
$High\_TFP_{jt}$	0.051**	0.124***	0.275***	0.228***
	(0.014)	(0.033)	(0.023)	(0.025)
$Turb_t * High\_TFP_{jt}$	-1.088***	-1.648***	-1.737***	-1.466***
	(0.128)	(0.219)	(0.180)	(0.180)
$constant$	0.072***	0.093***	0.033***	0.041***
	(0.008)	(0.013)	(0.007)	(0.007)
Firm Fixed Effect	Yes	Yes	Yes	Yes
Year Fixed Effect	Yes	Yes	Yes	Yes
Observations	20,931	20,861	20,624	20,426

Note: This table shows the estimation results from the empirical specification that regresses firm-level variables (including the growth rates of employment, capital expenditure, sales, and firm value) on the measured turbulence ($Turb$) for firms with different levels of TFP. The dummy $High\_TFP_{jt}$ equals one if firm j's TFP is above the median within its industry and zero otherwise. All regressions use the pseudo panel of Compustat firms that appear for at least 25 years from 1958 to 2015. The standard errors shown in the parentheses are clustered by industry. The stars denote the p-values: $^{*}p < 0.1$; $^{**}p < 0.05$; $^{***}p < 0.01$.

firms relative to those for low-productivity firms. The point estimates imply that a one-standard-deviation increase in turbulence reduces the relative growth rates of employment and capital for high-productivity firms by about 14.9 percent and 9.7 percent, respectively. It also reduces the relative growth rates of sales and the market value for high-productivity firms by about 4.9 and 5.6 percent, respectively.[14] Thus, turbulence has important impact

---

[14]The standard deviation of our measured turbulence is 2.6 percent. The impact of a one-standard-deviation increase in turbulence (from its mean level of 0.1) on the relative employment growth rate for high-productivity firms is thus $(-1.088) \times 0.1 \times 2.6 \approx -0.283$ percentage points, or about 14.9 percent drop from the average growth rate of 1.9% for high-productivity firms. Similarly, the impact on the relative growth rates of capital, sales, and market values are $(-1.648) \times 0.10 \times 2.6/4.4 \approx -9.7\%$, $(-1.737) \times 0.10 \times 2.6/9.4 \approx -4.9\%$, and $(-1.466) \times 0.10 \times 2.6/6.8 \approx -5.6\%$, respectively.

on firm-level activity, with greater adverse effects on high-productivity firms than on low-productivity firms. These findings suggest that turbulence reallocates capital and labor from high- to low-productivity firms, contributing to reducing aggregate TFP.[15]

III.3. **Financing constraints and the reallocation effects of turbulence.** To examine the extent to which the reallocation effects of turbulence might depend on financial frictions, we estimate the empirical specification

$$x_{it} = \beta_0 + \beta_1 High\_FF_{it} + \beta_2 Turb_t * High\_FF_{it} + \mu_i + \eta_t + \epsilon_{it}, \tag{6}$$

where the dependent variable x_{it} denotes interquartile range (IQR) of labor (or capital) of firms in industry i in year t, $Turb_t$ denotes measured turbulence, and $High\_FF_{it}$ is a dummy variable that equals one if industry i's external financing dependence is above the median level among all NAICS 4-digit industries in year t. We measure a firm's external financing dependence using the Kaplan- Zingales (KZ) index following Kaplan and Zingales (1997) and Lamont et al. (2001). We obtain an industry-level measure of financing dependence by taking the within-industry sales-weighted average of the firm-level KZ indices. To mitigate potential biases associated with firm entries and exits, we focus on the sample with firms appearing 25+ years from 1958 to 2016 (Sample 2). In estimating (6), we control for industry fixed effects (μ_i) and year fixed effects (η_t). The term ϵ_{it} denotes regression errors.

Changes in the IQR of employment (or capital) capture reallocations within an industry. For example, a decline in the IQR of employment following an increase in turbulence would indicate reallocation of labor from firms with high levels of employment to those with low levels of employment. We are interested in how financial frictions could affect the reallocation effects of turbulence. This effect is captured by the parameter β_2 in Eq. (6), which measures the relative sensitivity of industry-level dispersions of employment (or capital) to changes in turbulence for industries with high levels of external financing dependence. The parameter β_1 measures the average effect of financing dependence on the IQR of employment or capital. The estimation results are displayed in Table 3.

In the baseline specifications for the IQRs of both employment and capital (Columns (1) and (3)), the estimated values of β_2 are negative and statistically significant at the 99 percent confidence level. Thus, an increase in turbulence is associated with relative declines in the cross-sectional dispersions of employment and capital in industries with high levels of external financing dependence. Absent turbulence, the dispersions of employment and

---

[15]In the Appendix, we show that our results are robust to alternative samples with large industries, and also to alternative indicators of high productivity firms based on the firms' TFP ranking with one-year lag or using finer grouping of firms based on their TFP rankings. See Tables A.1, A.2, and A.3 in the Appendix.

TABLE 3. Reallocation effect of turbulence: sensitivity to financial frictions

Dep. Var.	IQR of Employment		IQR of Capital	
	(1)	(2)	(3)	(4)
$High\_FF_{it}$	0.932***	1.039***	0.959***	1.144***
	(0.288)	(0.278)	(0.320)	(0.319)
$Turb_t * High\_FF_{it}$	-8.201***	-9.486***	-9.428***	-11.222***
	(2.602)	(2.540)	(2.957)	(2.905)
constant	2.162***	2.193***	2.545***	2.573***
	(0.037)	(0.037)	(0.045)	(0.044)
Industry Fixed Effect	Yes	Yes	Yes	Yes
Year Fixed Effect	Yes	Yes	Yes	Yes
Observations	4,575	4,472	4,575	4,472

Note: This table shows the regression of interquartile range of employment (or capital) on the measured turbulence ($Turb$) for industries with different levels of external financing dependence. In the baseline specification (Columns (1) and (3)), the dummy $High\_FF_{it}$ equals one if industry i's external financing dependence is above the median. In the alternative specification (Columns (2) and (4)), we use lagged indicator of external financing dependence (i.e., $High\_FF_{i,t-1}$ instead of $High\_FF_{it}$). All regressions use the pseudo panel of Compustat firms that appear for at least 25 years in the sample from 1958 to 2015. The standard errors shown in the parentheses are clustered by industries. The stars denote the p-values: $^* p < 0.1$; $^{**} p < 0.05$; $^{***} p < 0.01$.

capital are positively related with the industry-level financing dependence, as indicated by the positive estimates of β_1.

For robustness, we also consider a lagged indicator of external financing dependence (i.e., $High\_FF_{i,t-1}$ instead of $High\_FF_{it}$). The estimation results (reported in Columns (2) and (4)) confirm that financial constraints are important for the reallocation effects of turbulence. Tighter financial constraints are associated with larger declines in the cross-sectional dispersions of employment and capital when turbulence rises.[16]

---

[16]In the Appendix, we show that our results are also robust to finer grouping of industries based on their external financing dependence (see Table A.4).
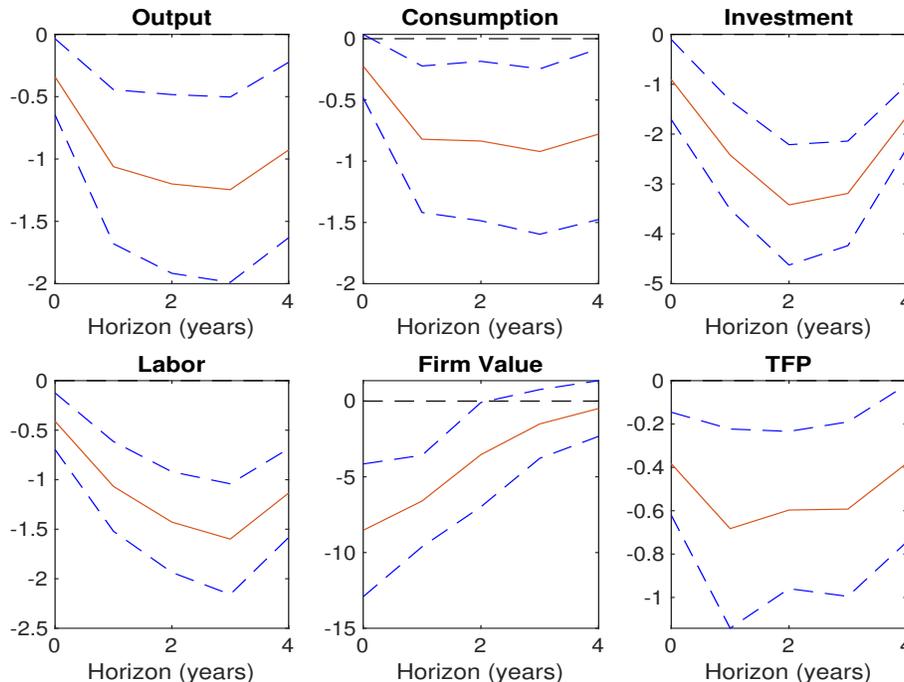
FIGURE 3. Estimated impulse response of macroeconomic variables to a turbulence shock

Note: This figure shows the impulse responses of macroeconomic variables to a one-standard-deviation (20.94%) increase in the log-level of turbulence estimated from the local projections model (7). The solid lines show the point estimates of the impulse responses. The blue dashed lines show the 68% confidence intervals.
Source: BEA, Compustat, NBER-CES, and authors' calculations.

III.4. **Macroeconomic effects of turbulence.** We now examine the macroeconomic effects of turbulence. For this purpose, we estimate the impulse responses of several key macroeconomic variables to a turbulence shock using the local projections approach of Jordà (2005).

We consider the empirical specification

$$x_{t+h} - x_{t-1} = \beta_0^h + \beta_1^h turb_t + \beta_2^h turb_{t-1} + \beta_3^h (x_{t-1} - x_{t-2}) + \epsilon_{t+h} \quad h = 0, 1, 2, 3, 4. \quad (7)$$

The dependent variable $x_{t+h} - x_{t-1}$ denotes the cumulative changes in the log-level of the variable of interest from year $t-1$ to year $t+h$, where h denotes the projection horizons (number of years). The list of dependent variables includes the macroeconomic times series of per capita real consumption, investment, private output (i.e., the sum of consumption and investment), and hours worked, and also the firm value and the manufacture TFP constructed from the firm-level and industry-level data. The independent variable $turb_t \equiv \log(1 - \rho_t)$

denotes the log-level of turbulence in year t. In estimating the local projections, we control for lagged turbulence ($turb_{t-1}$) and the lagged growth rate of the dependent variable ($x_{t-1} - x_{t-2}$). The term ϵ_{t+h} is the regression residual. The parameter β_1^h measures the impulse responses of the macroeconomic variables to a turbulence shock at horizon h.

Figure 3 plots the estimated impulse responses of the macroeconomic variables to a one-standard-deviation turbulence shock (i.e., an increase in turbulence of 0.2094) for horizons up to five years.[17] The shock leads to a recession with synchronized and persistent declines in aggregate output, consumption, investment, hours worked, and firm value. It also leads to a decline in manufacturing TFP. These macroeconomic effects of turbulence are quantitatively important. For example, a one-standard-deviation increase in turbulence reduces per capita output by about 0.5 percent on impact, and by more than one percent within three years after the shock.

IV. A real business cycle model with turbulence shocks

We now construct a real business cycle model to examine the economic mechanism through which turbulence can drive macroeconomic fluctuations and cross-sectional reallocation. In light of the empirical evidence presented in Section III, we incorporate into the model two key ingredients—firm heterogeneity and financial frictions. We show that these ingredients are both important for the transmission of turbulence shocks.

IV.1. **The model.** The model economy is populated by a continuum of infinitely lived households with measure one. The representative household has the utility function

$$\mathbf{E} \sum_{t=0}^{\infty} \beta^t \left\{ \ln C_t - \psi \frac{N_t^{1+\gamma}}{1+\gamma} \right\}, \tag{8}$$

where C_t denotes consumption, N_t denotes labor hours, and $\mathbf{E}$ is an expectation operator. The parameter $\beta \in (0,1)$ is a subjective discount factor, $\psi > 0$ measures the relative weight on the disutility of working, and $\gamma \geq 0$ is the inverse Frisch elasticity of labor supply.

All markets are perfectly competitive. The household takes prices as given and maximizes the utility in Eq. (8) subject to the sequence of budget constraints

$$C_t + K_{t+1} = (R_t + 1 - \delta)K_t + W_t N_t + D_t - T_t, \tag{9}$$

where K_{t+1} denotes the end-of-period capital stock, R_t denotes the capital rental rate, W_t denotes the real wage rate, D_t denotes the dividend income from firms, and T_t denotes a lump-sum tax paid to the government.

---

[17]Our measured annual series of (logged) turbulence has a first-order autocorrelation of 0.606 and a standard deviation of 0.2633, implying a standard deviation of the innovation of 0.2094.

There is a continuum of firms, each endowed with a constant-returns technology that produces the final consumption good using capital and labor as inputs.[18] Firms face idiosyncratic productivity shocks drawn at the beginning of each period, before hiring inputs. The production function for an individual firm is given by

$$y_{jt} = A_t z_{jt} k_{jt}^{\alpha} n_{jt}^{1-\alpha}, \tag{10}$$

where y_{jt} denotes the output produced by firm j in period t, and k_{jt} and n_{jt} denote the capital and labor inputs, respectively.

The term A_t denotes an aggregate productivity shock that follows the AR(1) process

$$\ln(A_t) = \rho_A \ln(A_{t-1}) + \sigma_A \varepsilon_t^A, \tag{11}$$

where the innovation term ε_t^A follows the standard normal process. The parameter ρ_A and σ_A measure the persistence and the volatility, respectively, of the aggregate productivity shock.

The idiosyncratic productivity shock z_{jt} follows the stochastic process described in Eq. (2), which we rewrite here for convenience of referencing:

$$z_{j,t+1} = \begin{cases} z_{jt} & \text{with prob} \quad \rho_t, \\ \tilde{z} & \text{with prob} \quad 1 - \rho_t. \end{cases} \tag{12}$$

Here, the term $\tilde{z}$ is an i.i.d. random variable with a finite number of states. Specifically, we assume that $\tilde{z} = z_j$ with probability π_j, for $j = 1, 2, ..., J$. Without loss of generality, we further assume that $z_1 < z_2 < ... < z_J$. The process features time-invariant cross-sectional distribution of firm productivity such that, regardless of the realization of $\rho_t \in (0,1)$, there is always a fraction π_j of firms with $z_{jt} = z_j$ in each period. Thus, in a stationary equilibrium, π_j is the measure of firms with productivity z_j.

We measure turbulence by $1 - \rho_t$. If $\rho_t = 1$, then the idiosyncratic productivity z_{jt} would be permanent. If $\rho_t = 0$, on the other hand, then each firm would face i.i.d. shocks to productivity with no persistence. A lower value of ρ_t implies that a high-productivity firm in the current period may not maintain its productivity in the next period, whereas a low-productivity firm in the current period might be able to draw a better productivity in the next period. Thus, a decline in ρ_t reshuffles firms' productivity ranking across time, increasing turbulence.[19]

---

[18]In Appendix B, we show that the main model mechanism that drives the macroeconomic and reallocation effects of turbulence shocks is similar if the production technology exhibits decreasing returns of scale.

[19]As we have shown in Proposition 1, turbulence does not alter the *ex ante* stationary distribution of the idiosyncratic productivity. Thus, it is conceptually different from micro-level uncertainty such as that studied by Bloom et al. (2018).

We assume that the turbulence shock follows the stochastic process

$$\ln(1 - \rho_t) = (1 - \rho_\rho)\ln(1 - \bar{\rho}) + \rho_\rho \ln(1 - \rho_{t-1}) + \sigma_\rho \varepsilon_t^\rho, \tag{13}$$

where $\bar{\rho}$ denotes the average level of ρ_t and the innovation term ε_t^ρ follows a standard normal process. The parameter ρ_ρ and σ_ρ measure the persistence and the volatility of the turbulence shock, respectively.

Firms rely on external financing of their working capital. In the beginning of each period, firms need to borrow from a competitive financial intermediary to cover payments for input factors, and these working capital loans are repaid within the period, after firms receive revenues. Following Jermann and Quadrini (2012) and Liu and Wang (2014), we assume that a firm's borrowing capacity is constrained by a fraction θ of its expected equity value in the next period, in line with the empirical evidence of Lian and Ma (2021).

Firms at each level of productivity face idiosyncratic production distortions (denoted by τ_{jt}), reflecting differential policy interventions or government subsidies at the firm level (Restuccia and Rogerson, 2008; Hsieh and Klenow, 2009; Buera and Shin, 2013; Moll, 2014). These production distortions drive a wedge between firms' private and social marginal revenue products. We assume that τ_{jt} is drawn from a continuous i.i.d. distribution $F(\tau_{jt})$. Under credit constraints, the presence of idiosyncratic production distortions allows a fraction of firms at each level of productivity to stay active, enabling turbulence shocks to generate reallocation and endogenous fluctuations in aggregate TFP.[20]

The firms' optimizing problem is characterized by the Bellman equation

$$V_t(z_{jt}, \tau_{jt}) = \max_{k_{jt}, n_{jt}} \tau_{jt} A_t z_{jt} k_{jt}^\alpha n_{jt}^{1-\alpha} - R_t k_{jt} - W_t n_{jt} + \mathbb{E}_t M_{t+1} V_{t+1}(z_{jt+1}, \tau_{jt+1}), \tag{14}$$

subject to the working capital constraint

$$R_t k_{jt} + W_t n_{jt} \leq \theta \mathbb{E}_t M_{t+1} V_{t+1}(z_{jt+1}, \tau_{jt+1}) \equiv \theta B_{jt}. \tag{15}$$

Here, the term $V_t(z_{jt}, \tau_{jt})$ denotes the value function of firm j that depends on the firm-level state variables z_{jt} and τ_{jt}. The value function $V_t(z_{jt}, \tau_{jt})$ also depends on aggregate shocks, which are summarized by the time subscript t. The term $M_{t+1} = \beta \frac{C_t}{C_{t+1}}$ denotes the stochastic discount factor determined by the marginal utilities of the representative household who owns all firms. The term B_{jt} denotes the expected present value of a firm with current productivity z_{jt}.

---

[20]Including idiosyncratic distortions also serves a technical purpose in our model with a discrete distribution of idiosyncratic productivity. The continuity of the distribution function $F(\tau_{jt})$ implies a well-defined cutoff point τ_{jt}^* that determines the subset of active firms at each level of productivity z_{jt}.

Profit maximizing implies the conditional factor demand functions

$$\alpha \frac{\tau_{jt} y_{jt}}{k_{jt}} = (1 + \mu_{jt}) R_t, \tag{16}$$

and

$$(1 - \alpha) \frac{\tau_{jt} y_{jt}}{n_{jt}} = (1 + \mu_{jt}) W_t, \tag{17}$$

where μ_{jt} denotes the Lagrangian multiplier associated with the credit constraint (15). Using the factor demand functions, we can write the firm's flow profit as

$$d_{jt} \equiv \left[\tau_{jt} A_t z_{jt} \left(\frac{\alpha W_t}{(1 - \alpha) R_t} \right)^{\alpha} - \frac{W_t}{1 - \alpha} \right] n_{jt}. \tag{18}$$

Since production subsidies follow an i.i.d. process, a firm would choose to be active in production if and only if its subsidy τ_{jt} is sufficiently high such that $d_{jt} \geq 0$. It follows that there exists a threshold level of production subsidy τ_{jt}^* such that, if $\tau_{jt} \geq \tau_{jt}^*$, then a firm would be active in production, facing binding credit constraints. Otherwise, the firm would remain inactive. At the threshold level of subsidy, a firm earns zero profit and thus it would be indifferent between producing and staying inactive. The indifference condition determines the threshold level of subsidy

$$\tau_{jt}^* = \frac{R_t^{\alpha} W_t^{1-\alpha}}{\alpha^{\alpha} (1 - \alpha)^{1-\alpha} A_t z_{jt}}. \tag{19}$$

The threshold τ_{jt}^* increases with the factor prices R_t and W_t and decreases with the productivity level z_{jt}. Thus, given the factor prices, the fraction of active firms is larger for firms with higher productivity.

The presence of credit constraints and production distortions creates misallocation of resources. Absent those distortions, all resources would be allocated to the most productive firm (with productivity z_J). However, under those distortions, some low-productivity firms are able to produce because not all high-productivity firms are active. Specifically, at each level of productivity, there is a non-degenerate fraction of firms that are active, with the share of active firms measured by $1 - F(\tau_{jt}^*)$ for all $j \in 1, \ldots, J$. Such misallocation opens up a reallocation channel for turbulence shocks, as we show below.

Since active firms face binding credit constraints and inactive firms do not use any input factors, we obtain the conditional demand functions for labor and capital inputs

$$n_t(z_{jt}, \tau_{jt}) = \begin{cases} \frac{(1-\alpha)\theta B_{jt}}{W_t}, & if \quad \tau_{jt} \geq \tau_{jt}^* \\ 0, & otherwise. \end{cases} \tag{20}$$

and

$$k_t(z_{jt}, \tau_{jt}) = \begin{cases} \frac{\alpha \theta B_{jt}}{R_t}, & if \quad \tau_{jt} \geq \tau_{jt}^* \\ 0, & otherwise. \end{cases} \tag{21}$$

Given the factor demand functions, firm j's value function can be written as

$$V_t(z_{jt}, \tau_{jt}) = \max\left\{\frac{\tau_{jt}}{\tau_{jt}^*} - 1, 0\right\}\theta B_{jt} + B_{jt}. \tag{22}$$

Since production subsidies are i.i.d. across time, the average value of a firm with productivity z_{jt} is given by

$$\bar{V}_t(z_{jt}) = \int V_t(z_{jt}, \tau)dF(\tau) = \left[1 + \theta \int_{\tau_{jt}^*} (\frac{\tau}{\tau_{jt}^*} - 1)dF(\tau)\right] B_{jt} \equiv \Phi(\tau_{jt}^*)B_{jt}, \tag{23}$$

where the term $\Phi(\tau_{jt}^*) \equiv 1 + \theta \int_{\tau_{jt}^*}(\frac{\tau}{\tau_{jt}^*} - 1)dF(\tau)$ is a decreasing function of the threshold subsidy level τ_{jt}^*.

Given the stochastic process of $z_{j,t+1}$ and the definition of B_{jt} in Eq. (15), we have

$$B_{jt} \equiv \beta\mathbb{E}_t\frac{C_t}{C_{t+1}}\left[\rho_t\bar{V}_{jt+1} + (1 - \rho_t)\sum_{i=1}^{J}\pi_i\bar{V}_{it+1}\right]. \tag{24}$$

In a competitive equilibrium, markets for labor, capital, and final consumptions goods all clear. Labor market clearing implies that

$$N_t = \sum_j \pi_j n_{jt} \equiv \sum_j \pi_j \frac{(1 - \alpha)\theta B_{jt}}{W_t}\left[1 - F(\tau_{jt}^*)\right]. \tag{25}$$

Capital market clearing implies that

$$K_t = \sum_j \pi_j k_{jt} \equiv \sum_j \pi_j \frac{\alpha\theta B_{jt}}{R_t}\left[1 - F(\tau_{jt}^*)\right]. \tag{26}$$

Goods market clearing implies that

$$Y_t = C_t + K_{t+1} - (1 - \delta)K_t, \tag{27}$$

where aggregate output Y_t is given by

$$Y_t \equiv \sum_j \pi_j y_{jt} = \sum_j \pi_j A_t z_{jt}k_{jt}^\alpha n_{jt}^{1-\alpha}. \tag{28}$$

Given aggregate output, aggregate capital and labor inputs, we define aggregate TFP as

$$Z_t \equiv \frac{Y_t}{K_t^\alpha N_t^{1-\alpha}} = \frac{\sum_j \pi_j A_t z_{jt}k_{jt}^\alpha n_{jt}^{1-\alpha}}{K_t^\alpha N_t^{1-\alpha}}. \tag{29}$$

Definition. A competitive equilibrium consists of the sequence of allocations $\{C_t, Y_t, N_t, K_t\}$ and the sequence of prices $\{W_t, R_t\}$ such that (i) taking all prices as given, the allocations solve the household's utility maximizing problem and the firms' profit maximizing problem; and (ii) markets for labor, capital, and goods all clear.
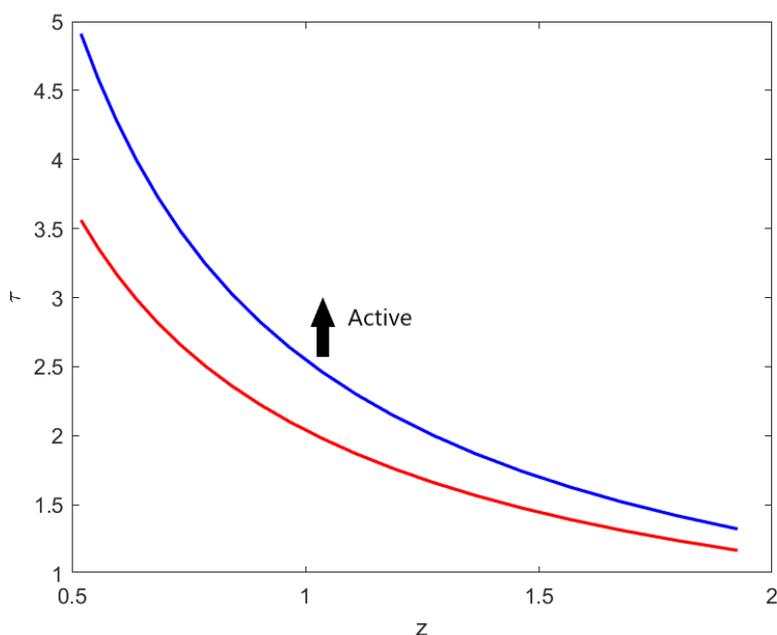
FIGURE 4. Production decisions in the steady-state equilibrium

Note: This figure shows the steady-state relation between the threshold level of subsidy τ^* and firm productivity z (blue line). Firms with (τ, z) lying above the threshold line are active in production and those below the line are inactive. The figure also shows the threshold line (red line) for production decisions in an economy with a higher average level of turbulence (i.e., a lower value of $\bar{\rho}$).

IV.2. **Steady-state allocations.** We now provide some analytical characterization of the steady-state equilibrium and show how the steady-state allocations vary with the average level of turbulence $(1 - \bar{\rho})$.

In Section IV.1, we have shown that a firm with productivity z_j chooses to produce (i.e., become active) if and only if its subsidy exceeds the threshold τ_j^*. The threshold level of subsidy is given by Eq. (19), and it is a decreasing function of firm productivity z_j.

Figure 4 illustrates the production decisions for firms with different levels of productivity (z) and subsidies (τ). The downward-sloping curve indicates the threshold function $\tau^*(z)$. At each z, a firm with a subsidy $\tau \geq \tau^*(z)$ chooses to produce. Otherwise, it stays inactive. Thus, the region of active firms are those with (τ, z) lying above the threshold curve.

In an economy with a higher average level of turbulence (i.e., with a lower value of $\bar{\rho}$), a high-productivity firm is less likely to remain productive, reallocating resources to low-productivity firms. Such reallocations reduce aggregate TFP, lowering the factor prices. For any given z, the declines in wages and capital rents reduce the threshold level of subsidy

τ^* (see Eq. (19)). Therefore, the threshold curve for production decisions shifts downward, with a flatter slope (red line), indicating that the increase in turbulence expands the active regions for low-productivity firms more than it does for high-productivity firms.

The reallocation effects of turbulence illustrated in Figure 4 can be formalized by the following proposition.

Proposition 2. Given the steady-state factor prices R and W, an increase in average turbulence reduces the share of labor hours allocated to high-productivity firms. Specifically, define the relative share of labor hours as $\eta_{ji} \equiv \frac{N_j}{N_i}$, where N_j and N_i denote labor hours allocated to active firms with productivity z_j and z_i, respectively. Without loss of generality, we assume that $z_j > z_i$. Then, we have

$$\frac{\partial \eta_{ji}}{\partial \bar{\rho}} > 0. \tag{30}$$

Proof. In the steady-state equilibrium, the relative share of labor is given by

$$\eta_{ij} = \frac{\pi_j}{\pi_i} \frac{1 - \beta\bar{\rho}\Phi(\tau_i^*)}{1 - \beta\bar{\rho}\Phi(\tau_j^*)} \frac{\left[1 - F(\tau_j^*)\right]}{\left[1 - F(\tau_i^*)\right]},$$

where we have used aggregated labor demand based on Eq. (20), with the term B_j substituted out using the steady-state version of Eq. (24).

At given values of W and R, the threshold τ_j^* is a function of z_j only. Since $z_j > z_i$, it is easy to show that $\Phi(\tau_j^*) > \Phi(\tau_i^*)$ and that $1 - F(\tau_j^*) > 1 - F(\tau_i^*) > 0$. Thus, we have

$$\frac{\partial \eta_{ji}}{\partial \bar{\rho}} = \frac{\beta[\Phi(\tau_j^*) - \Phi(\tau_i^*)]}{(1 - \beta\bar{\rho}\Phi(\tau_j^*))^2} \frac{\left[1 - F(\tau_j^*)\right]}{\left[1 - F(\tau_i^*)\right]} > 0 \tag{31}$$

$\square$

When turbulence rises ($\bar{\rho}$ declines), current productivity is less predictive for future productivity, such that productive firms are less likely to stay productive. Thus, an increase in turbulence lowers expected value of productive firms, reducing their borrowing capacity for financing working capital. As a consequence, labor is reallocated to less productive firms.

The analytical results in Proposition 2 are partial equilibrium in nature, because we have assumed that the factor prices W and R are independent of turbulence. However, since the production thresholds for firms with lower productivity are more sensitive to changes in the factor prices, an increase in turbulence that reduces the factor prices would disproportionally expand the active regions for low-productivity firms, reinforcing the misallocation effects of turbulence. We quantify the general equilibrium effects of a turbulence shock in the next section.

IV.3. **The calibration.** We solve the equilibrium dynamics numerically based on calibrated parameters. Table 4 displays the calibrated parameter values.

A period in our model corresponds to a quarter of a year. We set the subject discount factor to $\beta = 0.99$, implying an annualized risk-free interest rate of 4 percent. We calibrate the cost share of capital to $\alpha = 0.34$ using the NEBR-CES data following the approach of Bloom et al. (2018). We set the capital depreciation rate to $\delta = 0.025$ to match the average annual investment rate of 10 percent in the U.S. data (Eisfeldt and Rampini, 2006; Clementi and Palazzo, 2016). We set the inverse Frisch elasticity of labor supply to $\gamma = 5$. We calibrate the relative utility weight on leisure ψ such that the steady-state labor hours are one-third of the time endowment. We set the parameter θ to 0.35 to match the average ratio of working capital to market equity in the Compustat data.

We calibrate the turbulence shock process $1 - \rho_t$ based on the Spearman rank correlations of firm-level TFP (z_{jt}) using annual data from Compustat and NBER-CES (see Section III). The presence of production distortions (τ_{jt}) in the model can potentially complicate the calibration of ρ_t based on the Spearman correlation. However, since the production distortions τ_{jt} are i.i.d. (and thus serially uncorrelated), they do not affect the Spearman correlation, which measures the correlation of firms' rankings in the productivity distributions between adjacent periods.

In the data, the mean value of the Spearman correlation of firm-level TFP is about 0.90 at the annual frequency. Thus, we set the quarterly persistence of firm-level TFP to $\bar{\rho} = 0.9^{0.25} = 0.974$. The annual series of turbulence (in log levels) has a first-order autocorrelation of 0.606 and a standard deviation of 0.263. Translating to quarterly values, we obtain an autocorrelation of $\rho_\rho = 0.882$ and a standard deviation of the innovation of $\sigma_\rho = 0.124$.[21]

We assume that the idiosyncratic production distortion τ_{jt} follows a log-normal distribution with a positive support and a time-varying volatility. Specifically, we assume that the standard deviation of $\log(\tau_{jt})$ follows the stationary stochastic process

$$\ln(\sigma_{\tau,t}) = (1 - \rho_\sigma) \ln(\sigma_\tau) + \rho_\sigma \ln(\sigma_{\tau,t-1}) + \sigma_\sigma \varepsilon_t^\sigma, \tag{32}$$

where the innovation term ε_t^σ follows the standard normal process. The parameters ρ_σ and σ_σ measure the persistence and the standard deviation of the volatility shock, respectively. The uncertainty measure $\ln(\sigma_{\tau,t})$ here parallels the micro-level uncertainty in Bloom et al. (2018).

---

[21]The quarterly autocorrelation is thus given by $\rho_\rho = 0.606^{0.25} = 0.882$. The standard deviation of the innovation to the turbulence shock at the annual frequency is $0.263 * \sqrt{(1 - 0.606^2)} = 0.209$. Converting this to the quarterly frequency, the standard deviation of the shock innovation is $\sigma_\rho = \frac{0.209}{\sqrt{1 + \rho_\rho^2 + \rho_\rho^4 + \rho_\rho^6}} = 0.124$.

We calibrate the average volatility to $\sigma_\tau = 0.60$ to match the observed average IQR of employment across firms from 1960 to 2015 (the average IQR is 17). We normalize the mean value of $log(\tau_{jt})$ to $\mu_\tau = -0.5\sigma_\tau^2$ such that the unconditional mean of τ_{jt} is one (i.e., $E(\tau_{jt}) = 1$).

Given the calibrated process of τ_{jt}, we calibrate the volatility of the idiosyncratic productivity shock $\tilde{z}_{jt}$ based on our measured firm-level TFP. Our revenue-based measure of firm-level TFP includes both exogenous technology shocks z_{jt} and production distortions τ_{jt}. Specifically, the model implies that

$$tfp_{jt} = \log(z_{jt}) + \log(\tau_{jt}), \tag{33}$$

where tfp_{jt} is the firm-level TFP (in log units) that we have constructed based on the production function. The standard deviation of our measured tfp_{jt} is $\sigma_{tfp} = 0.607$. Given our assumption that $\log(z_{jt})$ and $\log(\tau_{jt})$ are independent processes, the unconditional standard deviation of $\log(z_{jt})$ (which is also the standard deviation of $\log(\tilde{z}_{jt})$) at the quarterly frequency is given by $\sigma_z = \sqrt{\sigma_{tfp}^2 - \sigma_\tau^2} = 0.05$.

We calibrate the parameters in the aggregate shocks following the literature. We set the quarterly persistence of aggregate TFP shocks to $\rho_A = 0.95$, following the real business cycle literature (Cooley and Prescott, 1995). We set the persistence of the micro-level uncertainty to $\rho_\sigma = 0.75$, consistent with Leduc and Liu (2016) and Bloom et al. (2018). We normalize the standard deviations of these aggregate shocks to 1 percent (0.01).

IV.4. **Impulse responses to a turbulence shock.** To examine the macroeconomic effects of turbulence shocks, we solve our model based on calibrated parameters. We simulate the model using third-order approximations of the equilibrium conditions around the deterministic steady-state. We then compute impulse responses of several key macroeconomic and distributional variables as deviations of those variables driven by the turbulence shock from their stochastic steady-state levels without the shock.[22]

Figure 5 displays the impulse responses to a one-standard-deviation shock to turbulence. An increase in turbulence reduces the chance for a current high-productivity firm to remain as productive in the future, and it also increases the chance for a current low-productivity firm

---

[22]We follow the approach in Fernández-Villaverde et al. (2011) and Leduc and Liu (2016) to compute the impulse responses. In particular, the model is first simulated for a large number of periods to compute the ergodic mean of each variable. It is then simulated using the ergodic means as a starting point. Finally, impulse responses to a turbulence shock are computed as the differences between the simulated path with the turbulence shock and the path with no shocks. This solution approach helps capture potential non-linear effects of the shock. Since turbulence shocks in our model have first-moment impact, the impulse responses generated from the third-order approximations are essentially the same as those from first-order approximations (and we have verified this).

TABLE 4. Calibrated parameters

	Parameter Description	Value	Target
β	Subjective discount factor	0.99	Average real interest rate of 4% per year
α	Capital share	0.34	Average cost share of capital (NBER-CES)
δ	Capital depreciation rate	0.025	Capital depreciation rate of 10% per year
γ	Inverse Frisch elasticity	5	Frisch elasticity of labor supply of 0.2
ψ	Utility weight on leisure	1396	Average hours of 1/3 of time endowment
θ	Loan to value ratio	0.35	Working capital to equity ratio (Compustat)
$\bar{\rho}$	Firm-level TFP persistence	0.974	Estimated (Compustat and NBER-CES)
ρ_ρ	Persistence of turbulence shock	0.8823	Estimated (Compustat and NBER-CES)
σ_ρ	Volatility of turbulence shock	0.124	Estimated (Compustat and NBER-CES)
μ_τ	Average production distortion (log)	-0.18	Estimated (Compustat and NBER-CES)
σ_τ	Volatility of production distortion (log)	0.60	Estimated (Compustat and NBER-CES)
σ_z	Volatility of firm-level TFP shock	0.05	Estimated (Compustat and NBER-CES)
ρ_A	Persistence of productivity shock	0.95	Cooley and Prescott (1995)
ρ_σ	Persistence of uncertainty shock	0.75	Bloom et al. (2018)
σ_A	Volatility of aggregate TFP shock	0.01	Normalized
σ_σ	Volatility of uncertainty shock	0.01	Normalized

to get a higher productivity draw in the future. Thus, the equity values of high-productivity firms declines relative to those of low-productivity firms, leading to a decline in the IQR of firm value and disproportionately tightening the borrowing capacity of high-productivity firms in the current period. Facing tightened credit constraints, high-productivity firms pull back hiring, reallocating labor and capital to low-productivity firms. Since high-productivity firms use more capital and labor in the steady-state than low-productivity firms, the increase in turbulence reduces the IQR of labor and capital across firms, and it also reduces the IQR of sales, in line with the empirical evidence presented in Section III.2.

Through reallocation, a turbulence shock reduces aggregate TFP and leads to a recession with synchronized declines in aggregate output, consumption, investment, and labor hours, as in the data. The recessionary effects of turbulence are sizable and persistent. For example, a one-standard-deviation turbulence shock leads to a drop in aggregate output of about 0.4 percent on impact, and output stays below its steady-state level for more than five years after the shock.

IV.5. **The role of financial frictions.** Our empirical evidence suggests that financial frictions are important for the reallocation effects of turbulence (Section III.3). We now illustrate
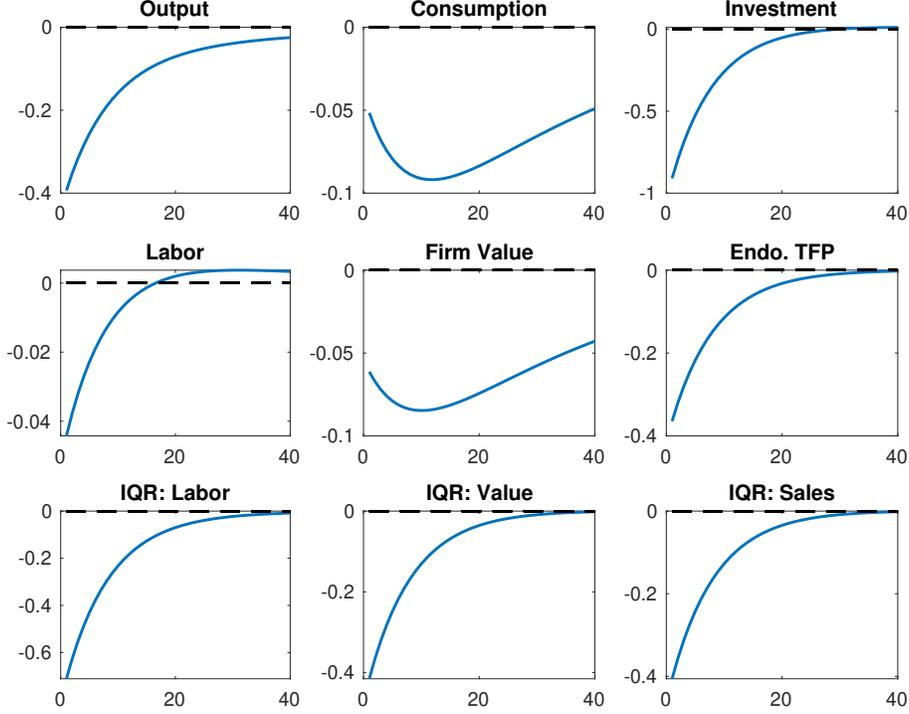
FIGURE 5. Impulse response to a turbulence shock in the benchmark model

Note: This figure shows the impulse responses to a one-standard-deviation shock to turbulence in the calibrated benchmark model. The horizontal axis shows the periods (quarters) since the impact of the shock. The vertical axis shows the percent deviations of each variable from its stochastic steady-state level.

the quantitative importance of financial frictions for propagating turbulence shocks to driven macroeconomic fluctuations. For this purpose, we consider a counterfactual version of our model, in which firms' borrowing capacity does not vary with the expected equity value. Specifically, we replace the working capital constraint with

$$R_t k_{jt} + W_t n_{jt} \leq \theta \beta E_t \frac{C_t}{C_{t+1}} \left[\rho_t \bar{V}_j^{ss} + (1 - \rho_t) \sum_{i=1}^{J} \pi_i \bar{V}_i^{ss} \right] \equiv \theta \bar{B}_{jt}, \qquad (34)$$

where $\bar{V}_j^{ss}$ denotes the steady-state equity value for firms with productivity z_{jt}. In this counterfactual, a turbulence shock can still influence firms' borrowing capacity by changing the transition probability (ρ_t) of the future productivity distribution, but changes in firms' expected equity value following a turbulence shock would have no effect on the borrowing capacity.

Figure 6 shows the impulse responses in the benchmark model (blue solid lines) and those in the counterfactual under this "quasi-fixed" borrowing capacity (red dash-dotted lines). The figure shows that the recession effects and the reallocation effects of a turbulence
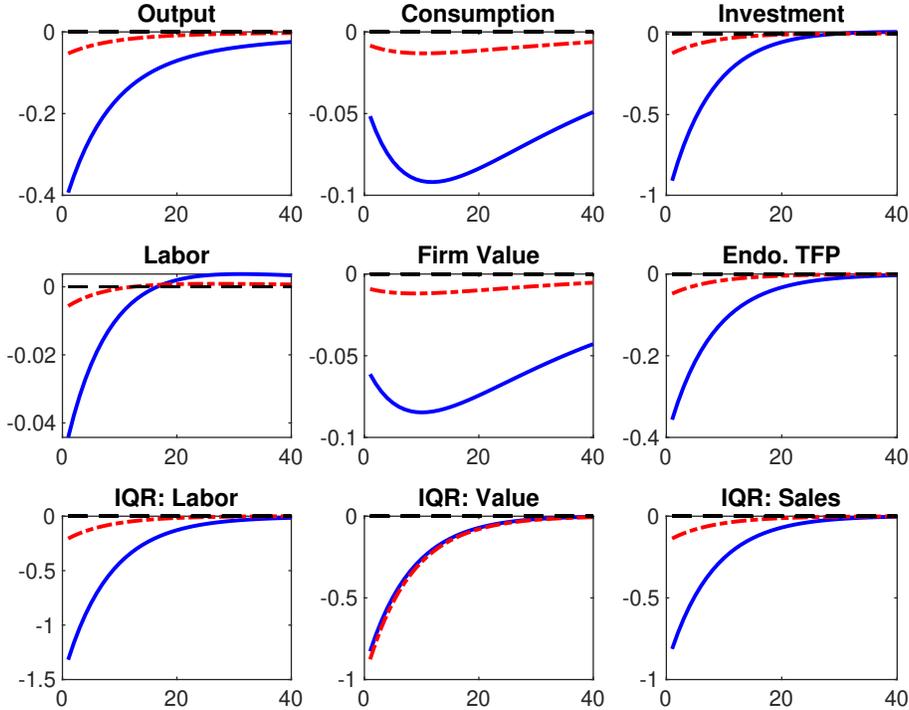
FIGURE 6. Impulse response to a turbulence shock: Benchmark model vs. counterfactual with quasi-fixed borrowing capacity

Note: This figure shows the impulse responses to a one-standard-deviation shock to turbulence in the benchmark model (blue lines) and in the counterfactual with quasi-fixed borrowing capacity (red dash-dotted lines). The horizontal axis shows the periods (quarters) since the impact of the shock. The vertical axis shows the percent deviations of each variable from its stochastic steady-state level.

shock would be substantially dampened if firms' borrowing capacity could not vary with the expected equity value. This counterfactual illustrates the importance of financial frictions—and in particular, the endogenous variations of the borrowing capacity with expected firm values—for propagating turbulence shocks.

IV.6. **Impulse responses to a micro-level uncertainty shock.** Turbulence is related to but different from micro-level uncertainty such as that studied by Bloom et al. (2018). Uncertainty increases the dispersion without changing the mean of the idiosyncratic firm-level shocks. Turbulence reshuffles firms' rankings in future productivity distributions, which also raises the *conditional* variance of the idiosyncratic shocks, but it does not change the ex ante *unconditional* distribution of productivity (see Proposition 1). More importantly, our model suggests that turbulence works through a reallocation channel stemming from financial frictions.
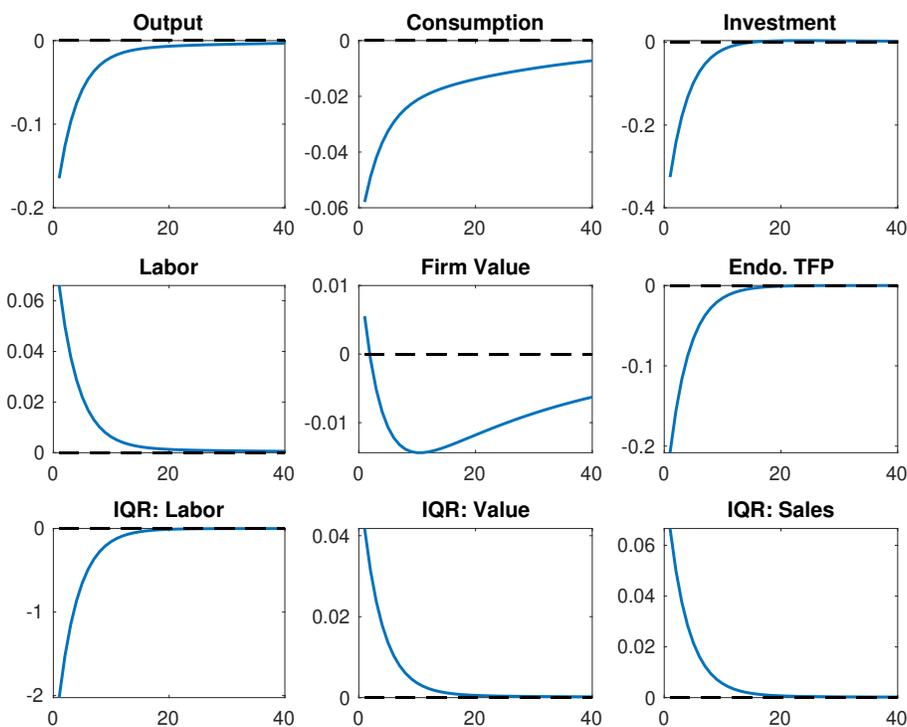
FIGURE 7. Impulse responses to a micro-level uncertainty shock in the benchmark model

Note: This figure shows the impulse responses to a one-standard-deviation shock to micro-level uncertainty in the benchmark model. Uncertainty is measured by the time-varying standard deviation of the production subsidies ($\sigma_{\tau,t}$). The horizontal axis shows the periods (quarters) since the impact of the shock. The vertical axis shows the percent deviations of each variable from its stochastic steady-state level.

To illustrate the relation between turbulence and uncertainty, we report in Figure 7 the impulse responses of the key macroeconomic and distributional variables following an increase in micro-level uncertainty, where we measure uncertainty by $\sigma_{\tau,t}$, the time-varying standard deviation of production subsidies.

Uncertainty leads to misallocation and reduces aggregate productivity. An increase in uncertainty expands the right tails of the subsidy distribution, raising the average subsidies for active firms at each productivity level (i.e., those with $\tau_j \geq \tau_j^*$).[23] Since the threshold level of subsidy (τ_j^*) decreases with firm-level productivity (z_j), the expansion of the right tail of the subsidy distribution increases the mass of active low-productivity firms by more than

---

[23]Uncertainty also expands the left tail of the distribution, but that does affect production because firms with subsidies in the left tails are inactive.

that of high-productivity firms.[24] Thus, uncertainty reallocates capital and labor towards low-productivity firms, reducing aggregate TFP. The decline in aggregate TFP contributes to the declines in output, consumption, and investment.

By increasing total subsidies for active firms, uncertainty induces more firms to stay active, boosting aggregate demand for labor and capital and raising wages and capital rents. Facing the increases in factor prices (that are common to all active firms), a low-productivity firm *on average* cuts back production more than a high-productivity firm. Thus, uncertainty raises the cross-sectional dispersion of firm-level sales (measured by the IQR of sales), as shown in Figure 7. Furthermore, since uncertainty induces a larger number of low-productivity firms to stay active, each low-productivity firm receives less subsidy *on average.* This also contributes to the increased IQR of sales and profitability (measured by firm value in the figure). In contrast, turbulence reduces the IQRs of both sales and firm value, partly because it does not affect the distribution of production subsidies.

Another important difference between the two types of shocks is that uncertainty boosts labor hours whereas turbulence reduces them. By raising the subsidies for active firms, an uncertainty shock shifts the labor demand curve upward, raising both the real wage rate and labor hours. Despite the increase in equilibrium labor hours, aggregate output declines because the decline in aggregate TFP more than offsets the increase in labor hours.[25]

For the same reason, uncertainty also raises demand for capital. Since the capital stock is predetermined, the capital rental rate rises persistently, creating an incentive for households to increase investment. However, uncertainty also reduces aggregate TFP through misallocation, generating a negative income effect. Under our calibration, the negative income effect dominates the intertemporal substitution effect, reducing equilibrium investment.[26]

---

[24]We discuss further details of the distributional effects of uncertainty in Appendix A.5.

[25]It is well-known that RBC models have difficulties in generating macroeconomic comovements following an uncertainty shock (Gilchrist and Williams, 2000). For example, the model in Bloom et al. (2018) implies a counterfactual increase in aggregate consumption following a micro-level uncertainty shock. They show that, to generate comovements in their model requires a simultaneous negative first-moment shock to TFP. Our model with financial frictions features a reallocation channel, through which uncertainty reduces aggregate TFP, and is thus more promising for generating aggregate comovements. However, under our calibration, uncertainty still boosts labor hours. New Keynesian models with sticky prices can generate comovements following an uncertainty shock (Basu and Bundick, 2017; Leduc and Liu, 2016).

[26]The responses of investment to uncertainty depend on calibrated parameters and, in particular, on the size of the elasticity of intertemporal substitution (EIS). Under a sufficiently large EIS, we find that the intertemporal substitution effect can dominate the income effect, such that investment increases following an uncertainty shock (not reported in the paper).

IV.7. **Impulse responses to an aggregate productivity shock.** The macroeconomic and reallocation effects of turbulence are also different from those associated with other aggregate shocks such as a TFP shock.

Figure 8 displays the impulse responses to a negative TFP shock. Similar to a turbulence shock, a negative TFP shock generates a recession with synchronized declines in aggregate output, consumption, investment, and labor hours. The shock also reduces average firm value.

However, the TFP shock has different reallocation effects than turbulence. A decline in aggregate TFP raises the threshold level of subsidy for active firms at each level of productivity, shrinking the set of active firms. Since labor and capital are perfectly mobile across firms, all firms face the same wages and capital rents. A decline in aggregate TFP would therefore force more low-productivity firms into the inactive regions than high-productivity firms. This "cleansing effect" reallocates resources to more productive firms, raising the endogenous component of aggregate TFP, mitigating the recession. The negative TFP shock also reduces firm value dispersion because, among active firms, lower-productivity firms need to be compensated by higher average subsidies for them to remain active. Thus, the average subsidy for low-productivity firms increases relative to that for high-productivity firms, reducing the dispersion in firm value.[27]

IV.8. **Quantitative importance of turbulence shocks.** Turbulence has quantitatively important recessionary effects, both in the model and in the data. In our quarterly model, a one-standard-deviation shock to turbulence leads to a drop in aggregate output of 0.4 percent and the recessionary effects persist for more than five years. Indeed, the magnitude of the recessionary effects of turbulence in the model is comparable to our empirical estimates discussed in Section III.4 .

Since our empirical measure of turbulence uses annual data, we calibrate an annual version of the model to facilitate comparisons of the impulse responses following a turbulence shock. In the annual model, we set the subjective discount factor to $\beta = 0.96$ and the capital depreciation rate to $\delta = 0.10$. We calibrate the turbulence shock process based on our empirical measure of turbulence. In particular, the annual series of our turbulence measure (in log units) has a mean of $log(0.1)$, a standard deviation of 0.2633, and a first-order autocorrelation of 0.606. The rest of the structural parameters are identical to those in the benchmark model.

Figure 9 compares the model-implied impulse responses of aggregate output (blue solid line) with the empirical estimates of the impulse response (black solid line). A one-standard-deviation turbulence shock reduces aggregate output by around 0.5 percent on impact, both

---

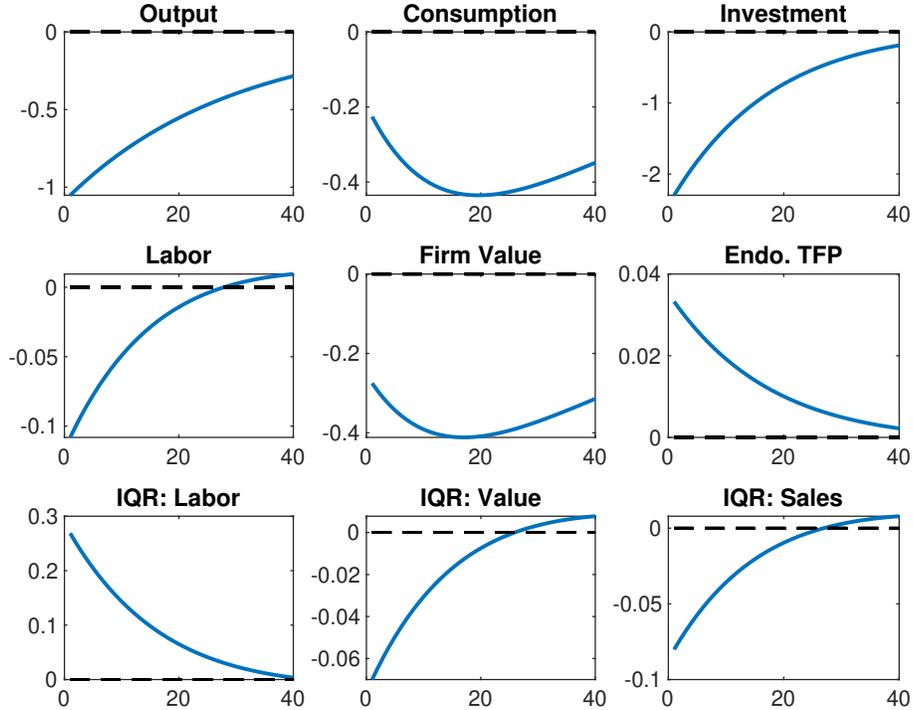[27]For distributional impacts of a TFP shock, see Figure A5 in Appendix A.6.

FIGURE 8. Impulse response to a negative aggregate TFP shock in the benchmark model

Note: This figure shows the impulse responses to a one-standard-deviation negative shock to aggregate TFP. The horizontal axis shows the periods (quarters) since the impact of the shock. The vertical axis shows the percent deviations of each variable from its stochastic steady-state level.

in the data and in the model. The shock has persistent recessionary effects on aggregate output both in the model and in the data, although the theoretical impulse responses miss the hump estimated from the data. These findings suggest that turbulence plays an important role in driving business cycles.[28]

V. POLICY INTERVENTIONS

Appropriate policy interventions can potentially undo the financial frictions, stabilizing aggregate output and improving allocative efficiency. To illustrate this point, we consider two alternative policy interventions in response to a recession driven by a turbulence shock.

---

[28]We have also compared the theoretical impulse responses of investment, consumption, and labor hours with those in the data (see Appendix A.7). We find that, similar to the case of output, the model-implied responses of investment and consumption are both in line with those estimated from the data, although the calibrated model fails to generate the turbulence-driven large declines in labor hours observed in the data.
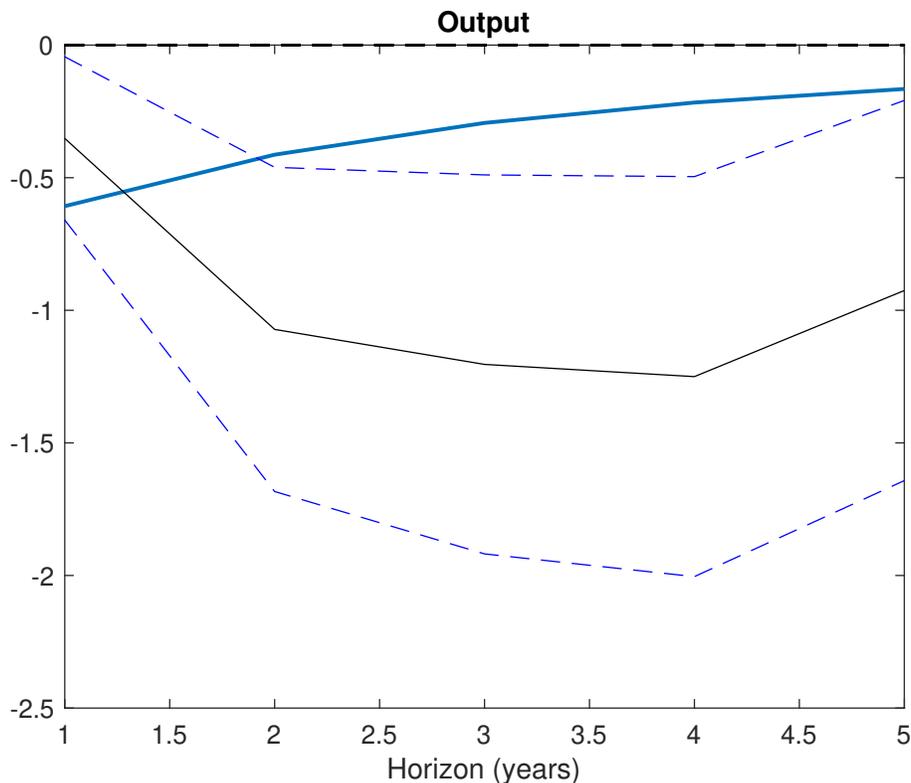
FIGURE 9. Impulse response to turbulence shock: Model vs. data

Note: This figure shows the impulse responses of private aggregate output to a one-standard-deviation shock to turbulence in the data (black solid line) and in the calibrated annual version of the model (blue solid line). The dashed lines show the 68% confidence band around the empirical estimates of the impulse responses. The horizontal axis shows the years after the impact of the shock. The vertical axis shows the percent deviations of output in the model from its steady-state level and the percentage changes in output in the data relative to its pre-shock level.

One policy is a borrowing subsidy that reduces firms' borrowing costs. The other is a credit-easing policy that expands firms' borrowing capacity.

Under the borrowing subsidy policy (Policy I), the government subsidizes wages and rents for active firms at an exogenous rate ω_{1t}, such that firms with productivity z_{jt} face the effective credit constraint

$$\tilde{R}_t k_{jt} + \tilde{W}_t n_{jt} \leq \theta B_{jt}, \tag{35}$$

where $\tilde{R}_t = (1 - \omega_{1t})R_t$ and $\tilde{W}_t = (1 - \omega_{1t})W_t$ denote the after-subsidy capital rental rate and real wage rate, respectively. The subsidies thus reduce the amount of working capital loans that firms need to borrow. The government finances the borrowing subsidies $\Omega_{1t} = \omega_{1t}(W_t N_t + R_t K_t)$ by imposing lump-sum taxes on the representative household. We

assume that operating this policy incurs a resource cost of $\lambda_1 \Omega_{1t}$, where $\lambda_1 \geq 0$ reflects potential deadweight losses associated with the government program.

Under the credit easing policy (Policy II), the government injects liquidity into active firms, such that firms with productivity z_{jt} face the effective credit constraint

$$R_t k_{jt} + W_t n_{jt} \leq \theta(1 + \omega_{2t}) B_{jt}, \tag{36}$$

where $\omega_{2t} B_{jt}$ is the amount of government transfers to active firms with expected equity value B_{jt}. The total cost of the credit-easing policy is given by $\Omega_{2t} = \omega_{2t} \sum_j \pi_j \theta B_{jt}[1 - F(\tau_{jt}^*)]$, which is financed by lump-sum taxes on the household. Similar to the borrowing subsidy policy, we assume that credit easing also incurs a resource cost of $\lambda_2 \Omega_{2t}$, where $\lambda_2 \geq 0$ reflects potential deadweight losses in operating the policy.

Following Bloom et al. (2018), we consider transitory and unanticipated policy interventions. A policy would be implemented only if a turbulence shock hits the economy, and the policy intervention has the same persistence as the shock. We evaluate the effectiveness of each of the two alternative policies—borrowing subsidies and credit easing—for mitigating the macroeconomic and reallocation effects of turbulence. For this purpose, we compare the impulse responses of aggregate output and aggregate TFP to a turbulence shock under borrowing subsidies (Policy I) or credit easing (Policy II) to those in the *laissez-faire* benchmark economy without policy intervention (No policy).

In each policy regime, we simulate the model economy for 1000 periods (quarters) based on third-order approximations of the equilibrium system around the deterministic steady-state. A turbulence shock and a simultaneous policy intervention (if any) are implemented in period 960. The unanticipated policy stimulus has a size of 3 percent of steady-state output, with the same persistence as the turbulence shock. After a policy intervention is implemented, we allow the economy to evolve naturally for the remaining 40 quarters. We calculate the responses of each endogenous variable to the turbulence shock (with or without a policy intervention) as percent deviations from the stochastic steady-state.

Figure 10 shows the stabilizing effects of the two alternative policies relative to the benchmark economy, conditional on a one-standard-deviation turbulence shock.[29] Compared to the benchmark economy without policy interventions (black bar), Policy I (red bar) is effective for stabilizing the declines in aggregate output (upper panel). By providing borrowing subsidies, the policy stimulates demand for labor and capital, and thus mitigating the declines in equilibrium hours, investment, and output. However, by reducing the effective

---

[29]The figure here shows the impact effects of a turbulence shock on aggregate output and TFP. The results are qualitatively the same when we consider the cumulative effects (not reported).
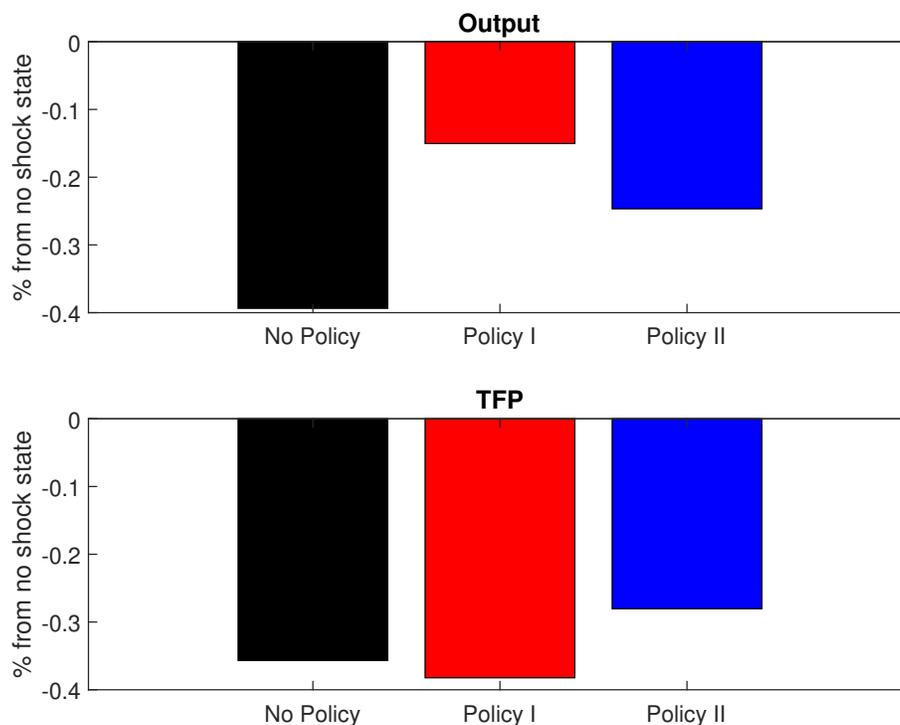
FIGURE 10. Impact effects of a turbulence shock with alternative policy interventions

Note: This figure plots the responses of aggregate output and aggregate TFP in the impact period of a one-standard-deviation turbulence shock. Black bars show the responses in the benchmark economy with no policy interventions. Red bars represent the responses under an unanticipated and temporary borrowing subsidy policy (Policy I). Blue bars represent the responses under an unanticipated and temporary credit easing policy (Policy II).

factor prices, Policy I enables a larger fraction of low-productivity firms to produce, exacerbating misallocation and intensifying the decline in aggregate TFP following a turbulence shock (lower panel).

The credit easing policy is also effective for stabilizing turbulence-driven output declines relative to the benchmark economy (blue bar, upper panel). The policy expands the borrowing capacity for all active firms, enabling a larger share of high-productivity firms to finance working capital and produce. The increase in the share of active high-productivity firms pushes up equilibrium wages and rents, shrinking the set of active low-productivity firms. Thus, Policy II reallocates labor and capital to high-productivity firms, improving aggregate TFP relative to the benchmark (blue bar, lower panel).

These policy experiments suggest that temporary borrowing subsidies or credit easing policies are effective for stabilizing turbulence-driven output fluctuations. However, the reallocation consequences of the two policies are different. While borrowing subsidies exacerbate misallocation, credit easing alleviates it.

VI. Conclusion

Macroeconomic fluctuations often mask underlying cross currents with important cross-sectional reallocations. We study the implications of turbulence—a form of reallocation shocks—for business cycles. An increase in turbulence changes the conditional distribution of firms' future productivity, leading to reallocations across firms. We measure turbulence based on firm-level TFP data and document evidence that turbulence is countercyclical, rising sharply in recessions. Turbulence has cross-sectional reallocation effects, the magnitude of which dependes on financial frictions. Turbulence is negatively correlated with average firm equity values and aggregate TFP. An increase in turbulence is associated with synchronized declines in aggregate output, consumption, investment, and labor hours.

Using a real business cycle model augmented with firm heterogeneity and financial frictions, we have highlighted a quantitatively important reallocation channel, through which a turbulence shock drives macroeconomic fluctuations. An increase in turbulence reduces the likelihood for the current high-productivity firms to maintain their productivity rankings in the future, lowering their expected equity values relative to those of the current low-productivity firms. Facing tightened working capital constraints, high-productivity firms pull back hiring of capital and labor relative to low-productivity firms, leading to reallocation from high- to low-productivity firms and reducing aggregate TFP. Such declines in TFP generate a recession with synchronized declines in aggregate output, consumption, investment, and labor hours, as in the data. A one-standard-deviation shock to turbulence leads to a drop in aggregate output of about 0.5 percent, with the recessionary effects persisting for more than five years, suggesting that turbulence plays an important role in driving business cycles.

Financial frictions are crucial for propagating turbulence shocks in our model. The presence of financial frictions also leads to misallocation. Policy interventions designed to alleviate credit constraints can potentially dampen the impact of turbulence and improve allocative efficiency. However, the particular approach to implementing such policy interventions can produce very different outcomes. For example, borrowing subsidies that reduce the amount of working capital loans that firms need to borrow can effectively boost aggregate output, mitigating the recessionary effects of turbulence. An alternative credit easing

policy that expands firms' borrowing capacity can also stimulate aggregate output. However, these two alternative policies have different implications for allocative efficiency. A borrowing subsidy enables more low-productivity firms to stay active, exacerbating misallocation, whereas credit easing allows high-productivity firms to expand production, improving aggregate productivity.

To illustrate the key transmission mechanism of turbulence, we have intentionally kept the model stylized. For example, the model abstracts from firm entries and exits. To the extent that firms rely on external financing and entering (exiting) firms have higher (lower) productivity than incumbent firms, we conjecture that introducing entry and exit decisions could potentially amplify the recessionary effects of turbulence through reallocation. Another direction of generalizing our study is to enrich the model by incorporating other real and nominal frictions such as habit formation, investment adjustment costs, and sticky prices and wages. With these additional frictions, the model can better fit time-series data and it can also be used to examine the role of monetary policy in stabilizing macroeconomic fluctuations driven by turbulence. We leave these important subjects for future research.

References

Aghion, P., N. Bloom, B. Lucking, R. Sadun, and J. Van Reenen (2021, January). Turbulence, firm decentralization, and growth in bad times. *American Economic Journal: Applied Economics 13*(1), 133–169.

Alfaro, I., N. Bloom, and X. Lin (2018, May). The finance uncertainty multiplier. NBER Working Paper No. 24571.

Arellano, C., Y. Bai, and P. J. Kehoe (2019). Financial frictions and fluctuations in volatility. *Journal of Political Economy 127*(5), 2049–1203.

Bachmann, R., S. Elstner, and E. R. Sims (2013). Uncertainty and economic activity: Evidence from business survey data. *American Economic Journal: Macroeconomics 5*(2), 217–49.

Baker, S. R., N. Bloom, and S. J. Davis (2016). Measuring economic policy uncertainty. *The Quarterly Journal of Economics 131*(4), 1593–1636.

Bansal, R., M. M. Croce, W. Liao, and S. Rosen (2019). Uncertainty-induced reallocations and growth. NBER Working Paper No. 26248.

Basu, S. and B. Bundick (2017). Uncertainty shocks in a model of effective demand. *Econometrica 85*(3), 937–958.

Berger, D., I. Dew-Becker, and S. Giglio (2020). Uncertainty shocks as second-moment news shocks. *Review of Economic Studies 87*(1), 40–76.

Bernanke, B. S., M. Gertler, and S. Gilchrist (1999). The financial accelerator in a quantitative business cycle framework. *Handbook of Macroeconomics 1*, 1341–1393.

Bernard, A. B. and T. Okubo (2016, September). Product switching and the business cycle. NBER Working Paper No. 22649.

Bloom, N. (2009). The impact of uncertainty shocks. *Econometrica 77*(3), 623–685.

Bloom, N. (2014). Fluctuations in uncertainty. *Journal of Economic Perspectives 28*(2), 153–76.

Bloom, N., M. Floetotto, N. Jaimovich, I. Saporta-Eksten, and S. J. Terry (2018). Really uncertain business cycles. *Econometrica 86*(3), 1031–1065.

Buera, F. J. and Y. Shin (2013). Financial frictions and the persistence of history: A quantitative exploration. *Journal of Political Economy 121*(2), 221–272.

Christiano, L. J., M. Eichenbaum, and C. L. Evans (2005). Nominal rigidities and the dynamic effects of a shock to monetary policy. *Journal of political Economy 113*(1), 1–45.

Christiano, L. J., M. S. Eichenbaum, and M. Trabandt (2018). On dsge models. *Journal of Economic Perspectives 32*(3), 113–140.

Christiano, L. J., R. Motto, and M. Rostagno (2014). Risk shocks. *American Economic Review 104*(1), 27–65.

Clementi, G. L. and B. Palazzo (2016). Entry, exit, firm dynamics, and aggregate fluctuations. *American Economic Journal: Macroeconomics 8*(3), 1–41.

Cooley, T. F. and E. C. Prescott (1995). *Frontiers of Business Cycle Research*, Volume 3. Princeton University Press Princeton, NJ.

David, J. M., H. A. Hopenhayn, and V. Venkateswaran (2016). Information, misallocation, and aggregate productivity. *The Quarterly Journal of Economics 131*(2), 943–1005.

David, J. M. and V. Venkateswaran (2019). The sources of capital misallocation. *American Economic Review 109*(7), 2531–67.

Davis, S. J., J. Haltiwanger, R. Jarmin, and J. Miranda (2006). Volatility and dispersion in business growth rates: Publicly traded versus privately held firms. *NBER Macroeconomics Annual 21*, 107–156.

Dou, W., Y. Ji, D. Tian, and P. Wang (2021). Costly misallocation: Endogenous growth and asset prices.

Eisfeldt, A. L. and A. A. Rampini (2006). Capital reallocation and liquidity. *Journal of Monetary Economics 53*(3), 369–399.

Fernández-Villaverde, J., P. Guerrón-Quintana, K. Kuester, and J. Rubio-Ramírez (2015). Fiscal volatility shocks and economic activity. *American Economic Review 105*(11), 3352–84.

Fernández-Villaverde, J., P. Guerrón-Quintana, J. F. Rubio-Ramírez, and M. Uribe (2011). Risk matters: The real effects of volatility shocks. *American Economic Review 101*(6), 2530–61.

Fernández-Villaverde, J. and P. A. Guerrón-Quintana (2020). Uncertainty shocks and business cycle research. *Review of Economic Dynamics 37*(S1), S118–S146.

Foster, L., J. Haltiwanger, and C. Syverson (2008). Reallocation, firm turnover, and efficiency: Selection on productivity or profitability? *American Economic Review 98*(1), 394–425.

Gertler, M. and S. Gilchrist (2018). What happened: Financial factors in the great recession. *Journal of Economic Perspectives 32*(3), 3–30.

Gertler, M. and P. Karadi (2011). A model of unconventional monetary policy. *Journal of monetary Economics 58*(1), 17–34.

Gertler, M. and N. Kiyotaki (2015). Banking, liquidity, and bank runs in an infinite horizon economy. *American Economic Review 105*(7), 2011–2043.

Gertler, M., N. Kiyotaki, and A. Queralto (2012). Financial crises, bank risk exposure and government financial policy. *Journal of Monetary Economics 59*, S17–S34.

Gilchrist, S., J. W. Sim, and E. Zakrajšek (2014, April). Uncertainty, financial frictions, and investment dynamics. NBER Working Paper No. 20038.

Gilchrist, S. and J. C. Williams (2000). Putty-clay and investment: A business cycle analysis. *Journal of Political Economy 108*(5), 928–960.

Hsieh, C.-T. and P. J. Klenow (2009). Misallocation and manufacturing tfp in china and india. *The Quarterly Journal of Economics 124*(4), 1403–1448.

Jermann, U. and V. Quadrini (2012). Macroeconomic effects of financial shocks. *American Economic Review 102*(1), 238–71.

Jordà, Ò. (2005). Estimation and inference of impulse responses by local projections. *American Economic Review 95*(1), 161–182.

Jurado, K., S. C. Ludvigson, and S. Ng (2015). Measuring uncertainty. *American Economic Review 105*(3), 1177–1216.

Kaplan, S. N. and L. Zingales (1997). Do investment-cash flow sensitivities provide useful measures of financing constraints? *The quarterly journal of economics 112*(1), 169–215.

Kiyotaki, N. and J. Moore (1997). Credit cycles. *Journal of Political Economy 105*(2), 211–248.

Lamont, O., C. Polk, and J. Saaá-Requejo (2001). Financial constraints and stock returns. *The review of financial studies 14*(2), 529–554.

Leduc, S. and Z. Liu (2016). Uncertainty shocks are aggregate demand shocks. *Journal of Monetary Economics 82*, 20–35.

Lian, C. and Y. Ma (2021). Anatomy of corporate borrowing constraints. *Quarterly Journal Economics 136*(1), 229–291.

Liu, Z. and P. Wang (2014). Credit constraints and self-fulfilling business cycles. *American Economic Journal: Macroeconomics 6*(1), 32–69.

Liu, Z., P. Wang, and Z. Xu (2021). Interest-rate liberalization and capital misallocations. *American Economic Journal: Macroeconomics 13*(2), 373–419.

Liu, Z., P. Wang, and T. Zha (2013). Land-price dynamics and macroeconomic fluctuations. *Econometrica 81*(3), 1147–1184.

Meier, M. (2020). Supply chain disruptions, time to build, and the business cycle. Technical report, University of Mannheim, Germany.

Midrigan, V. and D. Y. Xu (2014). Finance and misallocation: Evidence from plant-level data. *American Economic Review 104*(2), 422–58.

Moll, B. (2014). Productivity losses from financial frictions: Can self-financing undo capital misallocation? *American Economic Review 104*(10), 3186–3221.

Pratap, S. and E. Quintin (2011). Financial crises and labor market turbulence. *Journal of Monetary Economics 58*(6-8), 601–615.

Restuccia, D. and R. Rogerson (2008). Policy distortions and aggregate productivity with heterogeneous establishments. *Review of Economic dynamics 11*(4), 707–720.

Syverson, C. (2004). Market structure and productivity: A concrete example. *Journal of Political Economy 112*(6), 1181–1222.

APPENDIX A. ROBUSTNESS OF EMPIRICAL RESULTS AND ADDITIONAL RESULTS FROM THE BENCHMARK MODEL

This appendix presents some robustness checks on the empirical measurement of turbulence, the macroeconomic and allocative effects of turbulence, and some additional results from the calibrated model.

A.1. **Robustness of the turbulence measure.** Our measure of turbulence is robust to alternative measures of value added, capital input, and labor input. It is also robust to the data samples used.

In our benchmark empirical specification, we construct firm-level TFP based on firm-level value added and capital and labor inputs. We measure value added using firm-level sales and the average share of intermediate inputs at the 6 digit industry level, where the intermediate input share is the ratio of costs of materials to total value of shipments. We measure capital input using the real book value of a firm and labor input using the number of employees. We also focus on the sample that contains firms with 25+ years of observations (Sample 2). Figure A1 shows that the turbulence measure is robust to alternative measurements of value added, capital and labor inputs, and alternative samples.

The upper left panel of the figure compares the benchmark measure of turbulence (blue line) and the alternative measure using a different measure of value added (red line). In particular, we follow the approach in David et al. (2016) and David and Venkateswaran (2019), and construct value added by assuming a constant intermediate input share of 0.5 for all firms. These two alternative measures of turbulence are highly correlated, with a correlation coefficient of 0.8522. We have also considered another approach to constructing firm-level value added by subtracting the costs of goods sold from reported sales in Compustat (not shown in the figure). The resulting turbulence measure is also highly correlated with our benchmark measure, with a correlation coefficient of 0.7583.

The upper right panel of Figure A1 shows that the measure of turbulence is robust to alternative approaches to measuring capital. Here, instead of using the real book value of firms, we measure capital input by using a perpetual inventory method. Specifically, we first fix the initial real value of capital using $PPEGT$ in the first year of our sample. We then construct a measure of net investment using $PPENT_{it} - PPENT_{it-1}$, deflated by industry-specific investment deflators. Finally we iterate forward the law of motion of the capital stock by adding real net investment to the capital stock in the previous period. With this alternative measure of capital, we obtain a turbulence series (red line) that is highly correlated with the benchmark series (blue line), with a correlation coefficient of 0.9179.
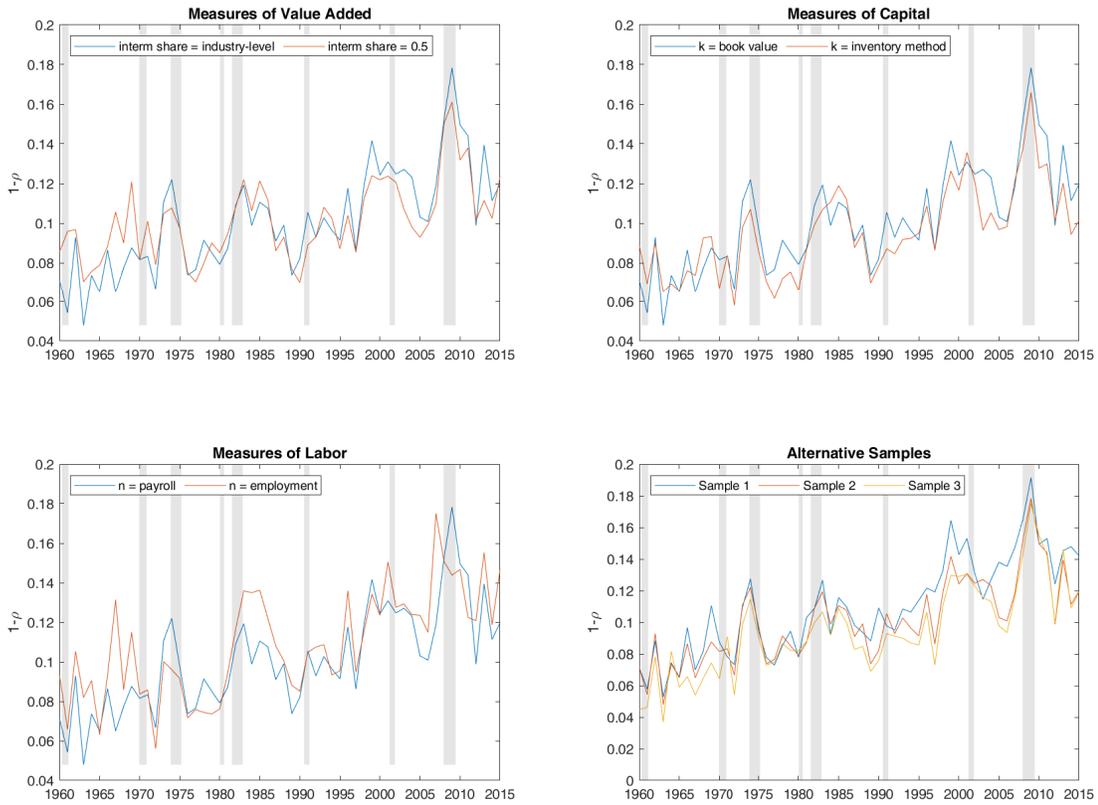
FIGURE A1. Robustness of Turbulence Measure

The measure of turbulence is also robust to alternative approaches to measuring labor input, as shown in the lower left panel of Figure A1. Here, instead of measuring labor input by the number of employees, we measure labor input by a firm's total payroll. The turbulence series under this alternative measure of labor input (red line) is highly correlated with the benchmark series (blue line), with a correlation coefficient of 0.7804.

Finally, the lower right panel of the figure shows that the turbulence measure is robust to alternative data samples.

A.2. **Robustness of the reallocation effects of turbulence.** We now show that the reallocation effects of turbulence are robust to our empirical specifications. In Table A.1 we consider an alternative sample with large industries, i.e. with at least 20 firms in each year.

It is possible that the current-year TFP ranking might be endogenous to employment, capital or sales growth. To address this issue, we construct an alternative indicator of high-productivity firms based on their TFP rankings with a one-year lag. We reestimate the responses of firm growth to turbulence shocks for firms with different levels of productivity.

TABLE A.1. Impact of turbulence on firms with different productivity

Dep. Var.	Δn_{jt}	Δk_{jt}	Δy_{jt}	Δv_{jt}
	(1)	(2)	(3)	(4)
$High\_TFP_{jt}$	0.053**	0.123**	0.282***	0.228***
	(0.016)	(0.040)	(0.026)	(0.028)
$Turb_t * High\_TFP_{jt}$	-1.112***	-1.701***	-1.714***	-1.447***
	(0.142)	(0.241)	(0.217)	(0.204)
constant	0.075***	0.098***	0.028***	0.040***
	(0.010)	(0.016)	(0.007)	(0.008)
Firm Fixed Effect	Yes	Yes	Yes	Yes
Year Fixed Effect	Yes	Yes	Yes	Yes
Observations	17,703	17,632	17,419	17,308

Note: This table shows the estimation results from the empirical specification that regresses firm-level variables (including the growth rates of employment, capital expenditure, sales, and firm value) on the measured turbulence ($Turb$) for firms with different levels of TFP. The dummy $High\_TFP_{jt}$ equals one if firm j's TFP is above the median within its industry and zero otherwise. All regressions use the pseudo panel of Compustat firms that appear for at least 25 years from 1958 to 2015, in industries with at least 20 firms in each year. The standard errors shown in the parentheses are clustered by industry. The stars denote the p-values: $^{*}p < 0.1$; $^{**}p < 0.05$; $^{***}p < 0.01$.

The results are shown in Table A.2. We find that, with this lagged high-TFP indicator, turbulence still reduces growth for high-productivity firms relative to low-productivity firms, as we found in the benchmark specification.

To examine the robustness of the reallocation effects of turbulence, we also consider an alternative specification in which we sort firm-level TFP into four quartiles and we replace the dummy $High\_TFP_{jt}$ in the baseline specification by the dummy indicators of the top three quartiles of the productivity distribution (denoted by $z_{2,j,t}$, $z_{3,j,t}$, and $z_{4,j,t}$) (Table A.3). Implicitly, we treat the firms in the first quartile ($z_{1,j,t}$) of the productivity distribution (i.e., firms with the lowest productivity levels) as the reference group. An increase in turbulence is associated with larger declines in employment, capital, sales and market value growth for

TABLE A.2. Impact of turbulence on firms with different productivity

Dep. Var.	Δn_{jt}	Δk_{jt}	Δy_{jt}	Δv_{jt}
	(1)	(2)	(3)	(4)
$High\_TFP_{jt-1}$	0.172***	0.232***	0.128***	0.166***
	(0.011)	(0.028)	(0.034)	(0.021)
$Turb_t * High\_TFP_{jt-1}$	-1.018***	-1.660***	-2.088***	-1.318***
	(0.099)	(0.172)	(0.179)	(0.226)
$constant$	0.007***	0.045***	0.131***	0.066***
	(0.002)	(0.005)	(0.015)	(0.004)
Firm Fixed Effect	Yes	Yes	Yes	Yes
Year Fixed Effect	Yes	Yes	Yes	Yes
Observations	20,043	20,041	20,043	19,543

Note: This table shows the regression of firm-level employment, capital expenditure, sales or firm value growth on the measured turbulence ($Turb$) for firms with different levels of TFP (lagged). The dummy $High\_TFP_{jt-1}$ equals one if firm j's TFP at year $t-1$ is above the median and zero otherwise. All regressions use the pseudo panel of Compustat firms that appear for at least 25 years from 1958 to 2015. The standard errors shown in the parentheses are clustered by industries. The stars denote the p-values: $^* p < 0.1$; $^{**} p < 0.05$; $^{***} p < 0.01$.

firms with higher productivity. These reallocation effects are both statistically significant and economically important.

A.3. **Robustness of the impact of financial friction on reallocation effects of turbulence.** To examine the robustness of the impact of financial friction on reallocation effects of turbulence, we also consider an alternative specification in which we sort industry-level external finance dependence into four quartiles and we replace the dummy $High\_FF_{it}$ in the baseline specification by the dummy indicators of the top three quartiles of the financial friction distribution (denoted by $FF_{2,it}$, $FF_{3,it}$, and $FF_{4,it}$) (Table A.4). Implicitly, we treat the industry in the first quartile ($FF_{1,it}$) of the external finance dependence distribution (i.e., industries with the lowest external finance dependence) as the reference group. An increase in turbulence is associated with larger declines in interquartile range of employment and capital for industries with higher external finance dependence. These effects are both statistically significant and economically important.

TABLE A.3. Impact of turbulence on firms with different productivity

Dep. Var.	Δn_{jt}	Δk_{jt}	Δy_{jt}	Δv_{jt}
	(1)	(2)	(3)	(4)
$z_{2,jt}$	0.049***	0.087***	0.265***	0.093**
	(0.016)	(0.018)	(0.035)	(0.038)
$z_{3,jt}$	0.012	0.102**	0.331***	0.203***
	(0.022)	(0.023)	(0.047)	(0.028)
$z_{4,jt}$	-0.016	0.113*	0.359***	0.254***
	(0.022)	(0.060)	(0.053)	(0.051)
$Turb_t * z_{2,jt}$	-0.941***	-1.141***	-1.658***	-0.648***
	(0.114)	(0.147)	(0.165)	(0.269)
$Turb_t * z_{3,jt}$	-0.992***	-1.451***	-1.820***	-1.208***
	(0.128)	(0.144)	(0.228)	(0.246)
$Turb_t * z_{4,jt}$	-1.010***	-1.635***	-1.456***	-1.388***
	(0.162)	(0.327)	(0.369)	(0.302)
$constant$	0.108***	0.113***	-0.019	0.031**
	(0.010)	(0.011)	(0.028)	(0.012)
Firm Fixed Effect	Yes	Yes	Yes	Yes
Year Fixed Effect	Yes	Yes	Yes	Yes
Observations	20,243	20,230	20,177	19,733

Note: This table shows the regression of firm-level employment, capital expenditure, sales and value growth on the measured turbulence ($Turb$) for firms with different levels of TFP. We sort the Compustat firms into four quartiles based on their TFP levels. The dummy variables $z_{2,jt}$, $z_{3,jt}$, and $z_{4,jt}$ indicate whether a firm j's TFP is in the second, third, or fourth quartile in year t. All regressions use the pseudo panel of Compustat firms that appear for at least 25 years from 1958 to 2015. The standard errors shown in the parentheses are clustered by industries. The stars denote the p-values: $^*p < 0.1$; $^{**}p < 0.05$; $^{***}p < 0.01$.

A.4. **Heterogeneous impacts of a turbulence shock.** Figure A2 shows that turbulence has heterogeneous effects on firms at different productivity levels. As discussed in the text, turbulence reduces aggregate TFP and leads to a recession. Thus, aggregate factor demand

TABLE A.4. Reallocation effects of turbulence: sensitivity to financial friction

Dep. Var.	IQR of Employment	IQR of Capital
	(1)	(2)
$FF_{2,it}$	0.575**	0.764**
	(0.283)	(0.337)
$FF_{3,it}$	0.907**	1.163***
	(0.346)	(0.418)
$FF_{4,it}$	1.592***	1.628***
	(0.385)	(0.458)
$Turb_t * FF_{2,it}$	-5.676**	-7.675**
	(2.573)	(3.210)
$Turb_t * FF_{3,it}$	-8.216**	-11.452***
	(3.287)	(4.443)
$Turb_t * FF_{4,it}$	-14.170***	-15.989***
	(3.580)	(4.046)
$constant$	2.159***	2.555***
	(0.057)	(0.070)
Industry Fixed Effect	Yes	Yes
Year Fixed Effect	Yes	Yes
Observations	4,575	4,575

Note: This table shows the regression of inter-quartile range of employment (or capital) on the measured turbulence ($Turb$) for industries with different levels of external finance dependence. We sort the NAICS four-digit industries into four quartiles based on their external finance dependence. The dummy variables $FF_{2,it}$, $FF_{3,it}$, and $FF_{4,it}$ indicate whether a industry i's KZ index is in the second, third, or fourth quartile in year t. All regressions use the pseudo panel of Compustat firms that appear for at least 25 years from 1958 to 2015. The standard errors shown in the parentheses are clustered by industries. The stars denote the p-values: $^* p < 0.1$; $^{**} p < 0.05$; $^{***} p < 0.01$.

declines, reducing wages and capital rents. At any given productivity level, the decline in the factor prices lowers the threshold level of subsidy for active production. Thus, the mass of producers at all levels of productivity increases, although the mass of high productivity firms
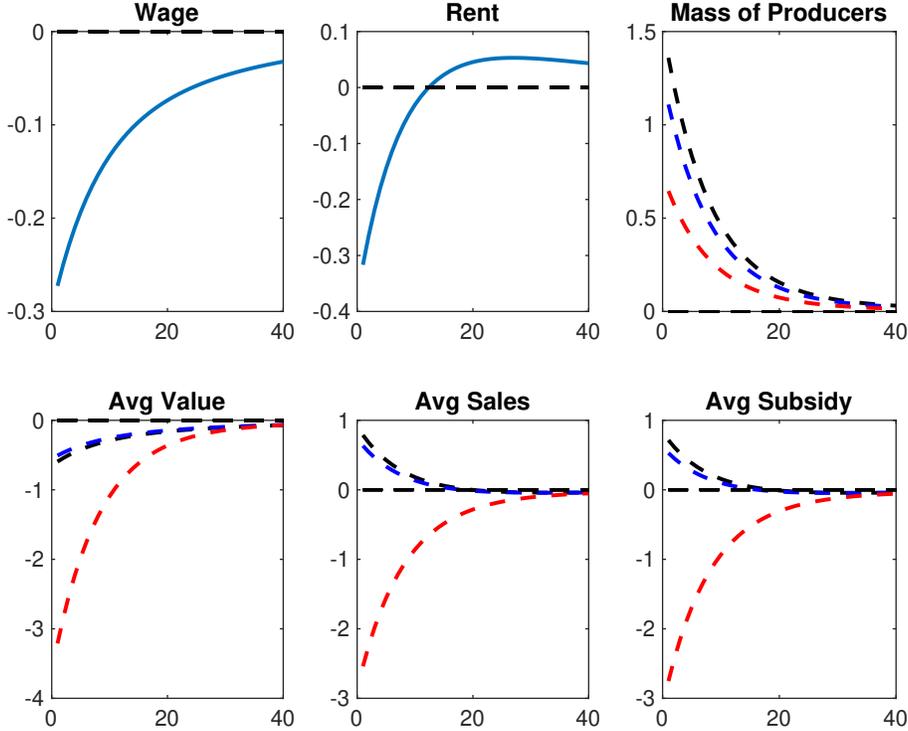
FIGURE A2. Heterogeneous impacts of a turbulence shock

This figure shows the impulse responses to a turbulence shock in the benchmark model. The black, blue and red dashed lines represent, respectively, the responses of firms at the 25, 50 and 100 percentiles of the productivity distribution. The horizontal axis shows the periods (quarters) after the impact of the shock. The vertical axis measures percent deviations from the stochastic steady-state in response to a one-standard-deviation shock to turbulence.

increases less because the shock that reshuffles productivity implies that higher-productivity firms are less likely to remain productive. Since all firms face the same factor prices, firms with lower productivity require higher subsidies to stay active. Therefore, average sales of active low-productivity firms increase relative to those of high-productivity firms, exacerbating misallocation.

A.5. **Heterogeneous impacts of a micro-level uncertainty shock.** An uncertainty shock measured by a mean-preserving increase in the volatility of the production subsidies $(\sigma_{\tau,t})$ expands the tails of the subsidy distribution. At each level of productivity z_{jt}, firms are active in production if and only if their actual subsidy exceeds a threshold level τ_{jt}^*. Since firms with subsidies below τ_{jt}^* stay inactive, uncertainty affects production decisions only through the expansion of the right tail of the subsidy distribution. At any given factor prices, τ_{jt}^* decreases with z_{jt} (see Eq. (19) in the text). Thus, high-productivity firms face a lower
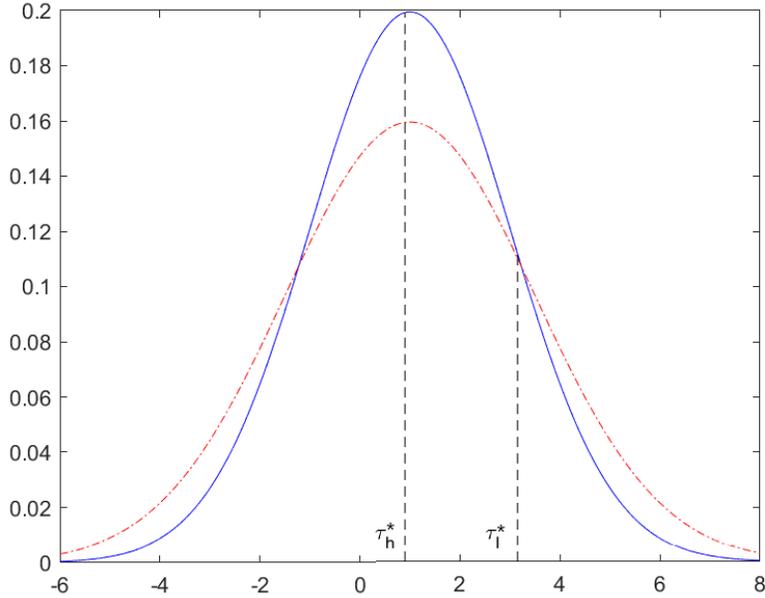
FIGURE A3. Impacts of an uncertainty shock on the distribution of active firms

This figure illustrates the impact of uncertainty shock on number of active firms in the benchmark model. The blue solid and red dashed curves represents the distribution of i.i.d. shock τ in the steady state and after a mean-preserving spread shock. τ_h^* and τ_l^* denote the thresholds of active production for high-productivity and low-productivity firms, respectively.

threshold than low-productivity firms. A right-tail expansion of the subsidy distribution will therefore increase the relative mass of low-productivity firms (relative to high-productivity firms). This is illustrated in Figure A3. To highlight our point, the figure shows a symmetric distribution, with the threshold for high-productivity firms (τ_h^*) normalized to be the mean of the distribution. The mass of high-productivity firms in this example is $1/2$, both before and after the uncertainty shock (because the shock is a mean-preserving spread). Since the threshold for low-productivity firms (τ_l^*) lies to the right of τ_h^*, the increase in uncertainty raises the mass of low-productivity firms.

Figure A4 shows that the micro-level uncertainty shock has heterogeneous impacts on firms with different levels of productivity. Uncertainty raises the average subsidies for active firms, boosting aggregate demand for labor and capital, and increasing wages and rents. The increase in the average subsidies for active firms induces more low-productivity firms to become active in production, increasing the relative mass of active low-productivity firms,
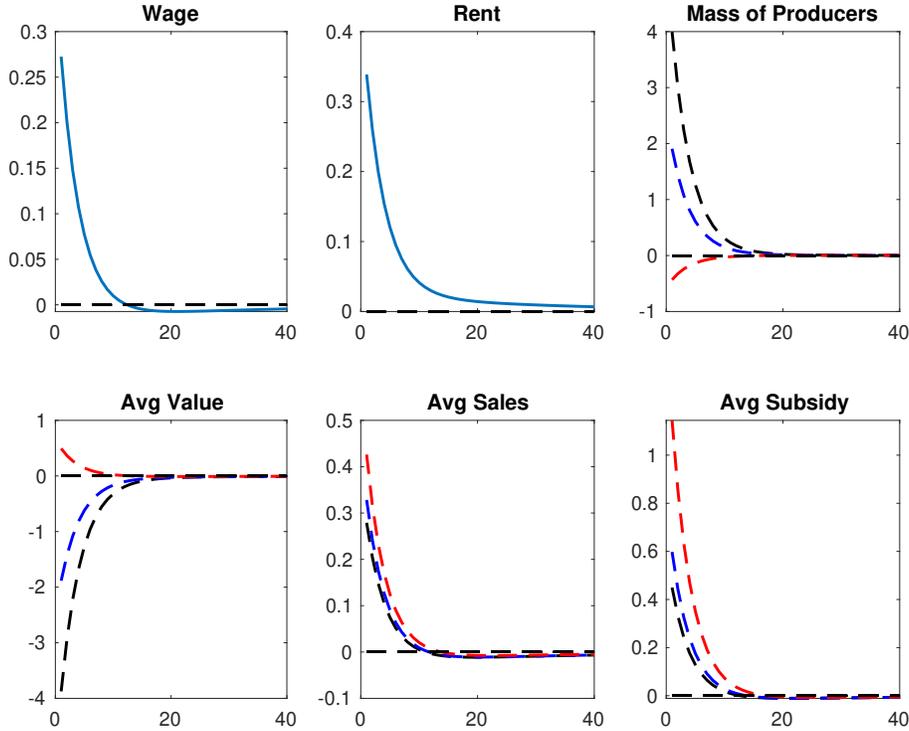
FIGURE A4. Heterogeneous impacts of an uncertainty shock

This figure shows the impulse responses to an uncertainty shock in the benchmark model. The black, blue and red dashed lines represent the responses of firms at the 25, 50, and 100 percentile of the productivity distribution. The horizontal axis shows the periods (quarters) after the impact of the shock. The vertical axis measures percent deviations from the stochastic steady-state in response to a one-standard-deviation shock to uncertainty.

exacerbating misallocation. The figure shows that uncertainty reduces the relative mass of the highest productivity firms (red dashed lines) to that of low productivity firms (black and blue lines). Since all firms face the same wages and rents, which are now higher than the steady-state, low-productivity firms face relatively high factor costs, such that *average* sales per active, low-productivity firm decline relative to those of high-productivity firms. This last effect also leads to an increase in the sales dispersion.

A.6. **Heterogeneous impacts of a TFP shock.** Figure A5 shows that a negative TFP shock has heterogeneous impacts on firms at different levels of productivity. The shock reduces aggregate labor and capital demand, lowering wages and capital rents. A decline in aggregate TFP raises the threshold of active production for firms at each level of productivity, shrinking the set of active firms, although this effect is partly mitigated by the decline in factor prices. Since labor and capital are perfectly mobile across firms, all firms face the
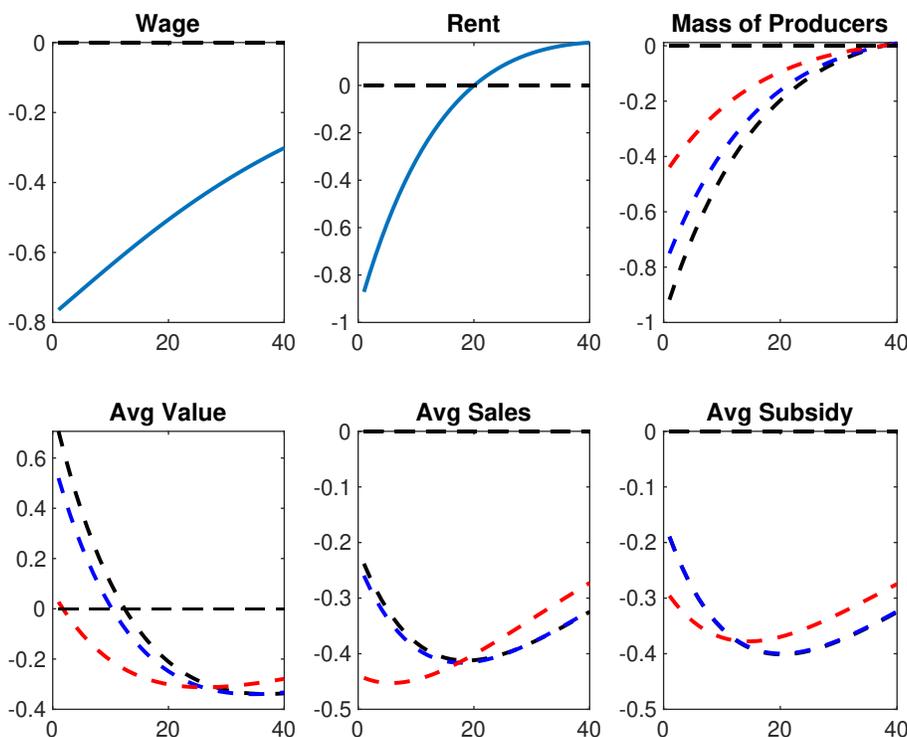
FIGURE A5. Heterogeneous impacts of a TFP shock

This figure shows the impulse responses to a TFP shock in the benchmark model. The black, blue and red dashed lines represent the responses of firms at the 25, 50, and 100 percentile of the productivity distribution. The horizontal axis shows the periods (quarters) after the impact of the shock. The vertical axis measures percent deviations from the stochastic steady-state in response to a one-standard-deviation shock to TFP.

same wages and capital rents. A decline in aggregate TFP would therefore force more low-productivity firms into the inactive regions than high-productivity firms. The shock reduces the average sales of all active firms, and average sales decline more for firms with higher productivity because, among active firms, lower-productivity firms need to be compensated by higher average subsidies for them to remain active.

A.7. **Macroeconomic effects of turbulence: Benchmark model vs. data.** In the text, we show that an annual version of the benchmark calibrated model generates empirically plausible impulse responses of aggregate output to a turbulence shock. Here, we compare the impulse responses of other macro variables to a turbulence shock from the model against those estimated from the data.

Figure A6 compares the impulse response of output, consumption, investment and hours worked to one-standard-deviation turbulence shock in the model (blue lines) vs. the data
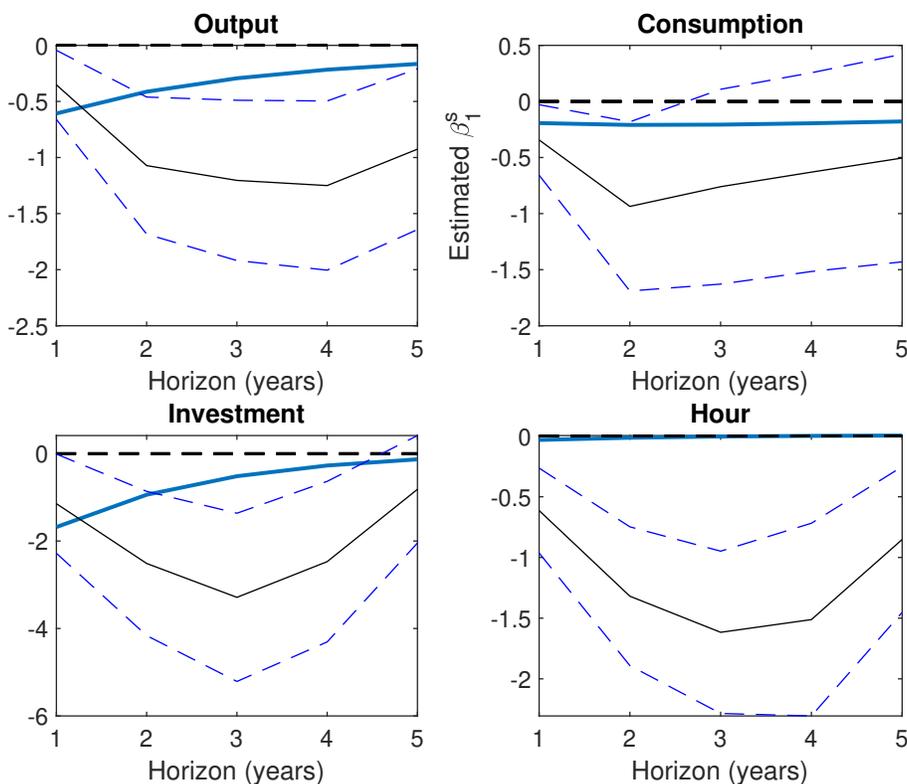
FIGURE A6. Impulse responses of macroeconomic variables to turbulence shock: Benchmark model vs. data

Note: This figure shows the impulse responses of aggregate output, consumption, investment, and labor hours to a one-standard-deviation shock to turbulence in the data (the black solid line) and in the calibrated annual version of the model (the blue solid line). The dashed lines show the 68% confidence band around the empirical estimates of the impulse responses. The horizontal axis shows the years after the impact of the shock. The vertical axis shows the percent deviations of output in the model from its steady-state level and the percentage changes in output in the data relative to its pre-shock level.

(black lines). The responses of output, investment, and consumption are close to those in the data in the sense that they lie within the 68% confidence bands of the empirical impulse responses (at least in the first two years). However, under the calibrated Frisch elasticity of labor supply (0.2), the model fails to generate the observed large contraction in labor hours following a turbulence shock.

APPENDIX B. DECREASING RETURNS TO SCALE

Now we consider an alternative version of RBC model with decreasing returns to scale (DRS) and show that a turbulence shock has similar reallocation and macroeconomic effects as in the benchmark model with a constant returns technology.

B.1. **The model.** The model economy is populated by a continuum of infinitely lived households with measure one, whose preference is characterized by the same utility function as in the benchmark model:

$$\mathbf{E} \sum_{t=0}^{\infty} \beta^t \left\{ \ln C_t - \psi \frac{N_t^{1+\gamma}}{1+\gamma} \right\}, \tag{A1}$$

All markets are perfectly competitive. The household takes all prices as given and maximizes the utility in Eq. (A1) subject to investment adjustment cost *a la* Christiano et al. (2005)

$$K_{t+1} = (1-\delta)K_t + [1 - \frac{\Omega_k}{2}(\frac{I_t}{I_{t-1}} - 1)^2]I_t \tag{A2}$$

such that the budget constraint becomes

$$C_t + I_t = R_t K_t + W_t N_t + D_t - T_t, \tag{A3}$$

where K_{t+1} denotes the end-of-period capital stock, R_t denotes the capital rental rate, W_t denotes the real wage rate, D_t denotes the dividend income from firms, and T_t denotes a lump-sum tax paid to the government.

Household's decision rules are characterized by the following equations:

$$\psi N_t^{\gamma} = \frac{1}{C_t} W_t \tag{A4}$$

$$1 = q_t \left(1 - \frac{\Omega_k}{2} \left(\frac{I_t}{I_{t-1}} - 1 \right)^2 - \Omega_k \left(\frac{I_t}{I_{t-1}} - 1 \right) \frac{I_t}{I_{t-1}} \right) + \beta E_t \frac{C_t}{C_{t+1}} q_{t+1} \Omega_k \left(\frac{I_{t+1}}{I_t} - 1 \right) \left(\frac{I_{t+1}}{I_t} \right)^2 \tag{A5}$$

where q_t is Tobin's q that measures return to capital and it satisfies

$$q_t = \beta E_t \frac{C_t}{C_{t+1}} \left(R_{t+1} + (1-\delta)q_{t+1} \right) \tag{A6}$$

There is a continuum of intermediate good firms, each endowed with a constant-returns technology that produces an intermediate good using capital and labor as inputs. Firms face idiosyncratic productivity shocks drawn at the beginning of each period, before hiring inputs. The production function for an individual firm is given by

$$y_{jt} = A_t z_{jt} k_{jt}^{\alpha} n_{jt}^{1-\alpha}, \tag{A7}$$

where y_{jt} denotes the output produced by firm j in period t, and k_{jt} and n_{jt} denote the capital and labor inputs, respectively. The term A_t and z_{jt} denote aggregate and idiosyncratic

productivity shocks respectively, which are assumed to follow the same stochastic processes as in the benchmark model.

Intermediate goods producers sell competitive monopolistic goods to a final good producer with production function as

$$Y_t = \left(\int_j [y_{jt}]^{\frac{\nu-1}{\nu}} dj \right)^{\frac{\nu}{\nu-1}}, \tag{A8}$$

from which we can derive demand function for each intermediate good as

$$p_{jt} = Y_t^{\frac{1}{\nu}} y_{jt}^{-\frac{1}{\nu}} \tag{A9}$$

Firms rely on external financing of their working capital, and face idiosyncratic production distortions (denoted by τ_{jt}). The firms' optimizing problem is characterized by the Bellman equation

$$V_t(z_{jt}, \tau_{jt}) = \tau_{jt} p_{jt} y_{jt} - W_t n_{jt} - R_t k_{jt} + E_t M_{t+1} V_{t+1}(z_{jt+1}, \tau_{jt+1}) \tag{A10}$$

subject to the working capital constraint

$$W_t n_{jt} + R_t k_{jt} \leq \theta E_t M_{t+1} V_{t+1}(z_{jt+1}, \tau_{jt+1}) \equiv \theta B_{jt} \tag{A11}$$

Profit maximizing implies

$$k_{jt} = \frac{\alpha}{1-\alpha} \frac{W_t}{R_t} n_{jt}. \tag{A12}$$

It follows that there exists a threshold level of production subsidy τ_{jt}^* such that, if $\tau_{jt} \geq \tau_{jt}^*$, then a firm would be facing binding credit constraints in production. Otherwise, the firm would choose an interior optimal size. At the threshold level of subsidy, the optimal size of production coincides with level implied from binding constraint. The indifference condition determines the threshold level of subsidy, τ_{jt}^*:

$$\tau_{jt}^* = \left[\frac{\theta B_{jt}}{(\frac{\nu-1}{\nu})^\nu \left[(\frac{1-\alpha}{W_t})^{1-\alpha} (\frac{\alpha}{R_t})^\alpha \right]^{\nu-1} (A_t z_{jt})^{\nu-1} Y_t} \right]^{\frac{1}{\nu}}, \tag{A13}$$

The threshold τ_{jt}^* increases with the factor prices R_t and W_t and decreases with the productivity level z_{jt}. Thus, given the factor prices, the fraction of active firms is larger for firms with higher productivity. Idiosyncratic labor demand functions are:

$$n_t(z_{jt}, \tau_{jt}) = \begin{cases} \frac{1-\alpha}{W_t} (\frac{\nu-1}{\nu})^\nu Y_t \tau_{jt}^\nu (A_t z_{jt})^{\nu-1} \left[(\frac{1-\alpha}{W_t})^{1-\alpha} (\frac{\alpha}{R_t})^\alpha \right]^{\nu-1}, & \text{if} \quad \tau_{jt} \leq \tau_{jt}^* \\ \frac{(1-\alpha)\theta B_{jt}}{W_t}, & \text{otherwise} \end{cases} \tag{A14}$$

Idiosyncratic capital demand functions are

$$k_t(z_{jt}, \tau_{jt}) = \begin{cases} \frac{\alpha}{R_t} (\frac{\nu-1}{\nu})^\nu Y_t \tau_{jt}^\nu (A_t z_{jt})^{\nu-1} \left[(\frac{1-\alpha}{W_t})^{1-\alpha} (\frac{\alpha}{R_t})^\alpha \right]^{\nu-1}, & \text{if} \quad \tau_{jt} \leq \tau_{jt}^* \\ \frac{\alpha\theta B_{jt}}{R_t}, & \text{otherwise} \end{cases} \tag{A15}$$

Idiosyncratic output functions are

$$
y_t(z_{jt}, \tau_{jt}) = \begin{cases} Y_t(\frac{\nu-1}{\nu}\tau_{jt}A_t z_{jt})^\nu \left[(\frac{1-\alpha}{W_t})^{(1-\alpha)}(\frac{\alpha}{R_t})^\alpha\right]^\nu, & \text{if} \quad \tau_{jt} \leq \tau_{jt}^* \\ A_t z_{jt} \left[(\frac{1-\alpha}{W_t})^{1-\alpha}(\frac{\alpha}{R_t})^\alpha\right]\theta B_{jt}, & otherwise \end{cases} \tag{A16}
$$

Since production subsidies are i.i.d. across time, the average value of a firm with productivity z_{jt} is given by

$$
\begin{aligned}
\bar{V}_{jt} &= \int V_t(z_{jt}, \tau)dF(\tau) = \frac{1}{\nu-1}(\frac{\nu-1}{\nu})^\nu Y_t(A_t z_{jt})^{\nu-1}\left[(\frac{1-\alpha}{W_t})^{1-\alpha}(\frac{\alpha}{R_t})^\alpha\right]^{\nu-1}\int^{\tau_{jt}^*}\tau^\nu dF(\tau) \\
&+ Y_t^{\frac{1}{\nu}}(A_t z_{jt})^{\frac{\nu-1}{\nu}}\left[(\frac{1-\alpha}{W_t})^{1-\alpha}(\frac{\alpha}{R_t})^\alpha z_{jt}\right]^{\frac{\nu-1}{\nu}}(\theta B_{jt})^{\frac{\nu-1}{\nu}}\int_{\tau_{jt}^*}\tau dF(\tau) - \theta B_{jt}[1-F(\tau_{jt}^*)] + B_{jt} \tag{A17}
\end{aligned}
$$

Given the stochastic process of $z_{j,t+1}$ and the definition of B_{jt} in Eq. (15), we have

$$
B_{jt} \equiv \beta\mathbb{E}_t\frac{C_t}{C_{t+1}}\left[\rho_t\bar{V}_{jt+1} + (1-\rho_t)\sum_{i=1}^J\pi_i\bar{V}_{it+1}\right] \tag{A18}
$$

In a competitive equilibrium, markets for labor, capital, and final consumption goods all clear. Labor market clearing implies that

$$
N_t = \sum_j \pi_j\left\{\frac{1-\alpha}{W_t}(\frac{\nu-1}{\nu})^\nu Y_t(A_t z_{jt})^{\nu-1}\left[(\frac{1-\alpha}{W_t})^{1-\alpha}(\frac{\alpha}{R_t})^\alpha\right]^{\nu-1}\int_0^{\tau_{jt}^*}\tau^\nu dF(\tau) + \frac{(1-\alpha)\theta B_{jt}}{W_t}[1-F(\tau_{jt}^*)]\right\} \tag{A19}
$$

Capital market clearing implies that

$$
K_t = \sum_j \pi_j\left\{\frac{\alpha}{R_t}(\frac{\nu-1}{\nu})^\nu Y_t(A_t z_{jt})^{\nu-1}\left[(\frac{1-\alpha}{W_t})^{1-\alpha}(\frac{\alpha}{R_t})^\alpha\right]^{\nu-1}\int_0^{\tau_{jt}^*}\tau^\nu dF(\tau) + \frac{\alpha\theta B_{jt}}{R_t}[1-F(\tau_{jt}^*)]\right\} \tag{A20}
$$

Final good market clearing condition implies

$$
Y_t = C_t + K_{t+1} - (1-\delta)K_t, \tag{A21}
$$

where

$$
y_{jt} = Y_t(\frac{\nu-1}{\nu}A_t z_{jt})^\nu\left[(\frac{1-\alpha}{W_t})^{(1-\alpha)}(\frac{\alpha}{R_t})^\alpha\right]^\nu\int_0^{\tau_{jt}^*}\tau^\nu dF(\tau) + A_t z_{jt}\left[(\frac{1-\alpha}{W_t})^{1-\alpha}(\frac{\alpha}{R_t})^\alpha\right]\theta B_{jt}[1-F(\tau_{jt}^*)] \tag{A22}
$$

Definition. A competitive equilibrium consists of the sequence of allocations $\{C_t, Y_t, N_t, K_t\}$ and the sequence of prices $\{W_t, R_t\}$ such that (i) taking all prices as given, the allocations solve the household's utility maximizing problem and the firms' profit maximizing problem; and (ii) markets for labor, capital, and goods all clear.

B.2. **Measured turbulence shock.** The methodology in estimation of turbulence can be easily extended to the decreasing return to scale (DRS) model. In specific, firm-level TFP is estimated from the following equation:

$$
tfp_{ijt} = y_{ijt} - \frac{\nu-1}{\nu}\alpha_{it}k_{ijt} - \frac{\nu-1}{\nu}(1-\alpha_{it})n_{ijt} \tag{A23}
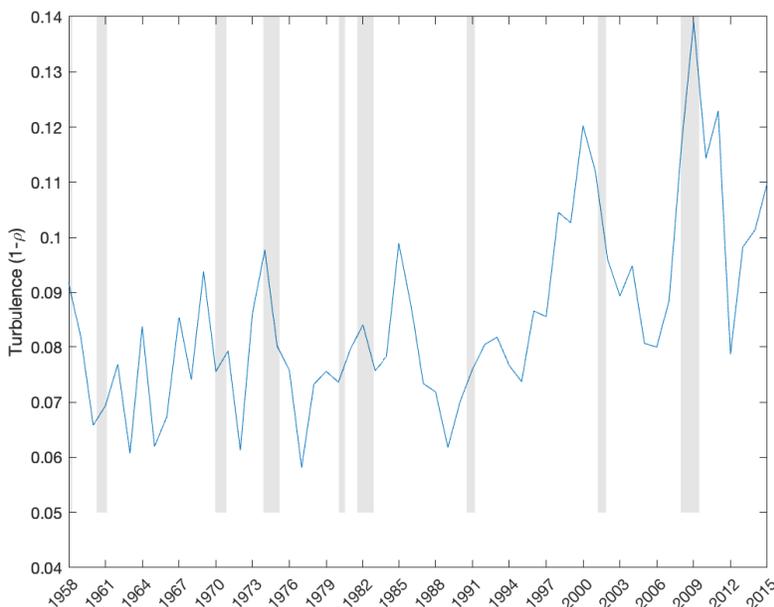$$

FIGURE A7. Measured micro-level turbulence (decreasing return to scale)

Note: Turbulence is measured by $1 - \rho_t$, where ρ_t is the Spearman correlation of firm TFP rankings between year t and year $t+1$. The gray shaded bars indicate NBER recession dates.

Source: Compustat, NBER-CES, BLS, and authors' calculations.

where ν measures elasticity of substitution. We follow standard New Keynesian literature to set $\nu = 10$, implying steady-state mark-up at around 1.1. The firm-level TFP are estimated after controlling for year fixed effect, which captures effect of aggregator Y_t on revenue of each firm. The rest of procedures strictly follow those adopted in constant return to scale model.

Time-varying turbulence in the model is measured by Spearman correlation of firm-level TFP ranking in decile within industry between two consecutive years, similar to measure constructed in figure A1 of Bloom et al. (2018). Figure A7 plots the time series of firm-level turbulence from 1958 to 2015.[30] The mean, standard deviation, and autocorrelation of the estimated ρ_t are 0.91, 0.017, and 0.641, respectively.

B.3. **Reallocation and macroeconomic effects of turbulence.** The measure of turbulence constructed under the DRS production function here has similar cyclical and reallocation effects as that under the CRS production function in the benchmark model.

---

[30]Our measure of turbulence is robust to alternative measures of value added, capital input, and labor input, as well as to the data samples used (not reported).

TABLE A.5. Impact of turbulence on firms with different levels of productivity

Dep. Var.	Δn_{jt}	Δk_{jt}	Δy_{jt}	Δv_{jt}
	(1)	(2)	(3)	(4)
$High\_TFP_{jt}$	0.054***	0.072***	0.198***	0.343***
	(0.008)	(0.016)	(0.017)	(0.048)
$Turb_t * High\_TFP_{jt}$	-1.268***	-1.333***	-1.880***	-3.525***
	(0.090)	(0.196)	(0.219)	(0.589)
$Constant$	0.057***	0.062***	0.025***	0.005
	(0.002)	(0.003)	(0.003)	(0.004)
Firm Fixed Effect	Yes	Yes	Yes	Yes
Year Fixed Effect	Yes	Yes	Yes	Yes
Observations	37,218	37,218	37,218	33,630

Note: This table shows the estimation results from the empirical specification that regresses firm-level variables (including the growth rates of employment, capital expenditure, sales, and firm value) on the measured turbulence ($Turb$) for firms with different levels of TFP under the DRS production function. The dummy $High\_TFP_{jt}$ equals one if firm j's TFP is above the median within its industry and zero otherwise. All regressions use the pseudo panel of Compustat firms that appear for at least 25 years from 1958 to 2015. The standard errors shown in the parentheses are clustered by industry. The stars denote the p-values: $^{*}p < 0.1$; $^{**}p < 0.05$; $^{***}p < 0.01$.

To examine the reallocation effects of turbulence, we re-estimate a regression (5) using the turbulence measure constructed from the DRS production function. Table A.5 shows the estimation results. The results show that an increase in turbulence is associated with declines in the firm-level growth rates for high-productivity firms relative to those for low-productivity firms.

The reallocation effects of turbulence also depend on financial frictions, as in our benchmark estimation. Specifically, Table A.6 shows the estimation results from the empirical specification (6) that is identical to that in the benchmark case, except that we use the measure of turbulence under the DRS technology. Again, we find that an increase in turbulence is associated with significant declines in the cross-sectional dispersions of employment and capital in industries with high levels of external financing dependence.

TABLE A.6. Reallocation effect of turbulence: sensitivity to financial frictions

Dep. Var.	IQR of Employment		IQR of Capital	
	(1)	(2)	(3)	(4)
$High\_FF_{it}$	1.022***	1.031***	1.243***	1.055***
	(0.305)	(0.271)	(0.395)	(0.338)
$Turb_t * High\_FF_{it}$	-8.800***	-8.962***	-11.440***	-9.377**
	(3.313)	(3.078)	(4.107)	(3.738)
constant	2.148***	2.463***	2.180***	2.501***
	(0.050)	(0.065)	(0.049)	(0.063)
Industry Fixed Effect	Yes	Yes	Yes	Yes
Year Fixed Effect	Yes	Yes	Yes	Yes
Observations	3,935	3,935	3,757	3,757

Note: This table shows the regression of interquartile range of employment (or capital) on the measured turbulence ($Turb$) for industries with different levels of external financing dependence. In the baseline specification (Columns (1) and (3)), the dummy $High\_FF_{it}$ equals one if industry i's external financing dependence is above the median. In the alternative specification (Columns (2) and (4)), we use lagged indicator of external financing dependence (i.e., $High\_FF_{i,t-1}$ instead of $High\_FF_{it}$). All regressions use the pseudo panel of Compustat firms that appear for at least 25 years in the sample from 1958 to 2015. The standard errors shown in the parentheses are clustered by industries. The stars denote the p-values: $^* p < 0.1$; $^{**} p < 0.05$; $^{***} p < 0.01$.

B.4. **Macroeconomic effects of turbulence.** To examine the macroeconomic effects of a turbulence shock, we re-estimate the local projections specification in Eq. (7) with the turbulence measure constructed under the DRS technology.

Figure A8 plots the estimated impulse responses of the macroeconomic variables to a one-standard-deviation turbulence shock (i.e., an increase in turbulence of 0.138) for horizons up to five years.[31] As in the benchmark case, a turbulence shock leads to a recession with synchronized and persistent declines in aggregate output, consumption, investment, hours worked, and firm value. It also leads to a decline in manufacturing TFP.

---

[31]Our measured annual series of (logged) turbulence has a first-order autocorrelation of 0.651 and a standard deviation of 0.182, implying a standard deviation of the innovation of 0.138.
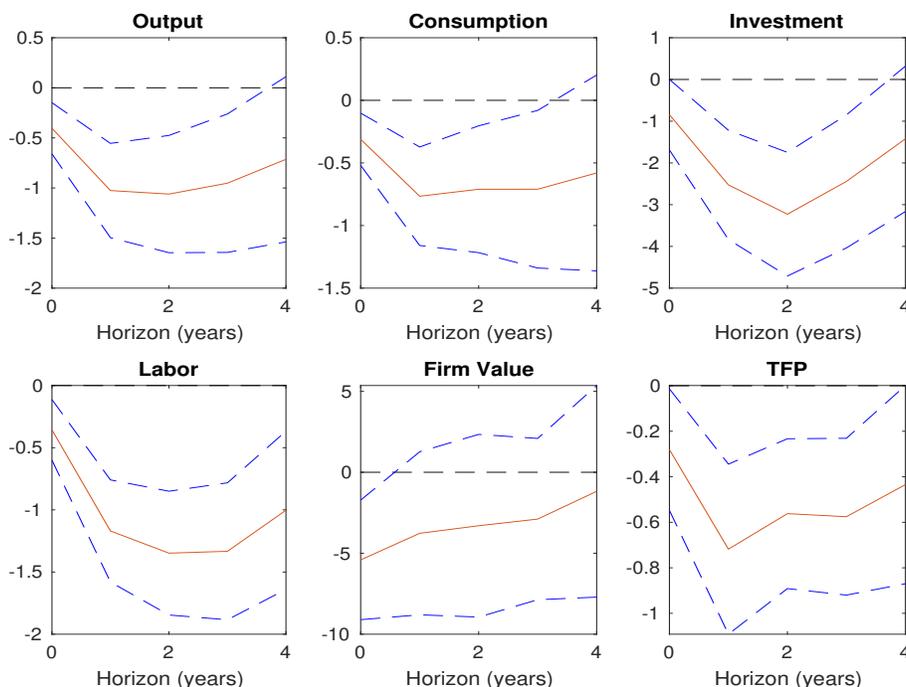
FIGURE A8. Estimated impulse response of macroeconomic variables to a turbulence shock

Note: This figure shows the impulse responses of macroeconomic variables to a one-standard-deviation (13.8%) increase in the log-level of turbulence estimated from the local projections model (7). The solid lines show the point estimates of the impulse responses. The blue dashed lines show the 68% confidence intervals.
Source: BEA, Compustat, NBER-CES, and authors' calculations.

B.5. **Quantitative impact of a turbulence shock in the RBC model.** We calibrate parameter values in the spirit of our benchmark model. We follow standard New Keynesian literature (e.g. Leduc and Liu (2016)) to set elasticity of substitution between differentiated goods $\nu = 10$, implying steady-state mark-up at around 1.1. We set the parameter Ω to 1 following the model of Christiano et al. (2005) [32]. Given the estimated TFP, we can back out parameters governing volatility of i.i.d. shocks following the same method as in benchmark case[33]. The parameters governing the process of turbulence are set to match mean, standard

---

[32]The estimated values of the investment adjustment cost parameter vary in the DSGE literature, for example 5.5 in Smets and Wouters (2007) or 2.00 in Liu, Waggoner, and Zha (2011) without financial frictions, and 0.17 in Liu et al. (2013) with credit constraints. Using these alternative values delivers similar quantitative results in our model.

[33]We calibrate the average volatility to $\sigma_\tau = 0.977$ to match the observed average IQR of employment across firms from 1960 to 2015 (the average IQR is around 15). We normalize the mean value of $log(\tau_{jt})$ to $\mu_\tau = -0.5\sigma_\tau^2$ such that the unconditional mean of τ_{jt} is one (i.e., $E(\tau_{jt}) = 1$). Given the calibrated

deviation and autocorrelation of ρ we estimated above. In the data, the mean value of the Spearman correlation of firm-level TFP is about 0.91 at the annual frequency. Thus, we set the quarterly persistence of firm-level TFP to $\bar{\rho} = 0.91^{0.25} = 0.9767$. The annual series of turbulence (in log levels) has a first-order autocorrelation of 0.651 and a standard deviation of 0.182. Translating to quarterly values, we obtain an autocorrelation of $\rho_\rho = 0.8982$ and a standard deviation of the innovation of $\sigma_\rho = 0.08$. [34] The rest parameters are set at the same value of benchmark model.

The qualitative impact of firm-level turbulence shock with decreasing return to scale is consistent with that in our baseline model. Figure A9 displays the impulse responses to a one-standard-deviation shock to turbulence. An increase in turbulence reduces the chance for a current high-productivity firm to remain as productive in the future, and it also increases the chance for a current low-productivity firm to get a higher productivity draw in the future. Thus, the equity values of high-productivity firms declines relative to those of low-productivity firms, leading to a decline in the dispersion of firm value and disproportionately tightening the borrowing capacity of high-productivity firms in the current period. Facing tightened credit constraints, high-productivity firms pull back hiring, reallocating labor and capital to low-productivity firms. Since high-productivity firms use more capital and labor in the steady-state than low-productivity firms, the increase in turbulence reduces the share of labor and capital in high-productivity firms, and it also reduces the dispersion of sales, in line with the empirical evidence presented in Section III.2.

Through reallocation, a turbulence shock reduces aggregate TFP and leads to a recession with synchronized declines in aggregate output, consumption, investment, and labor hours, as in the data. The recessionary effects of turbulence are sizable and persistent. For example, a one-standard-deviation turbulence shock leads to a drop in aggregate output of about 0.2

---

process of τ_{jt}, we calibrate the volatility of the idiosyncratic productivity shock $\tilde{z}_{jt}$ based on our measured firm-level TFP. Our revenue-based measure of firm-level TFP includes both exogenous technology shocks z_{jt} and production distortions τ_{jt}. Specifically, the model implies that

$$tfp_{jt} = \frac{\nu - 1}{\nu} \log(z_{jt}) + \log(\tau_{jt}), \tag{A24}$$

where tfp_{jt} is the firm-level TFP (in log units) that we have constructed based on the production function (after removing year fixed effect). The standard deviation of our measured tfp_{jt} is $\sigma_{tfp} = 1.01$. Given our assumption that $\log(z_{jt})$ and $\log(\tau_{jt})$ are independent processes, the unconditional standard deviation of $\log(z_{jt})$ (which is also the standard deviation of $\log(\tilde{z}_{jt})$) at the quarterly frequency is given by $\sigma_z = \sqrt{\sigma_{tfp}^2 - \sigma_\tau^2} = 0.1193$.

[34]The quarterly autocorrelation is thus given by $\rho_\rho = 0.651^{0.25} = 0.8982$. The standard deviation of the innovation to the turbulence shock at the annual frequency is $0.182 * \sqrt{(1 - 0.651^2)} = 0.1382$. Converting this to the quarterly frequency, the standard deviation of the shock innovation is $\sigma_\rho = \frac{0.1382}{\sqrt{1 + \rho_\rho^2 + \rho_\rho^4 + \rho_\rho^6}} = 0.08$.

percent on impact, and output stays below its steady-state level for more than five years after the shock.
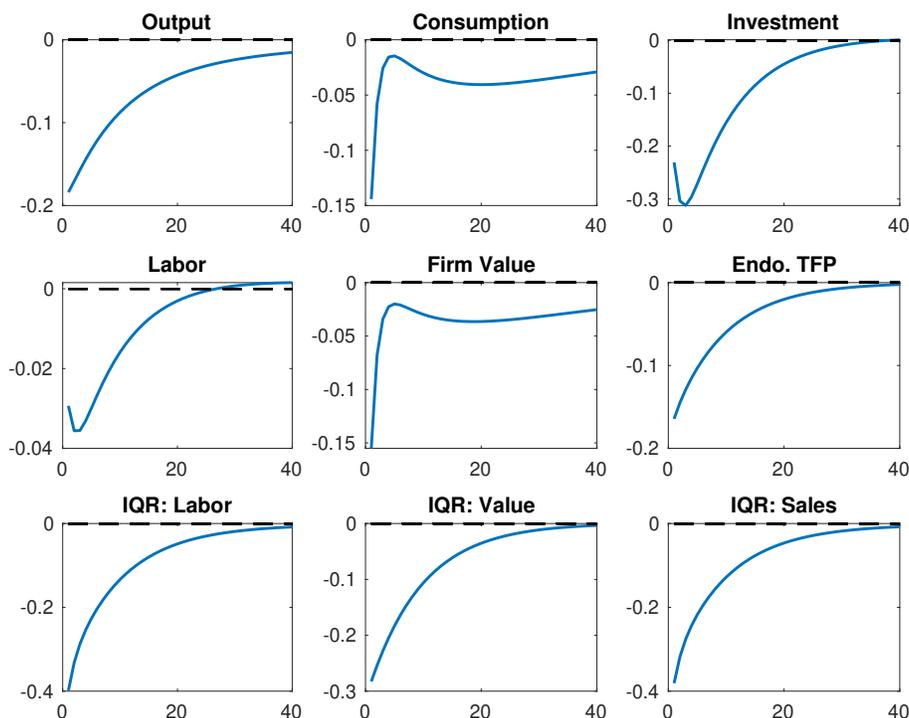

FIGURE A9. Impulse response to a turbulence shock in decreasing-return-to-scale model

Note: This figure shows the impulse responses to a one-standard-deviation shock to turbulence in the calibrated decreasing-return-to-scale model. The horizontal axis shows the periods (quarters) since the impact of the shock. The vertical axis shows the percent deviations of each variable from its stochastic steady-state level.

The role of financial frictions. As in the benchmark model, figure A10 shows that the recession effects and the reallocation effects of a turbulence shock would be substantially dampened if firms' borrowing capacity could not vary with the expected equity value. This counterfactual illustrates the importance of financial frictions—and in particular, the endogenous variations of the borrowing capacity with expected firm values—for propagating turbulence shocks.

Turbulence has quantitatively important recessionary effects, both in the model and in the data. We calibrate an annual version of the decreasing-return-to-scale model to facilitate comparisons of the impulse responses following a turbulence shock [35]. In the annual model,

[35]We re-estimate the macroeconomic effects of turbulence shock under decreasing-return-to-scale, by strictly following the local projection methods in the benchmark case.
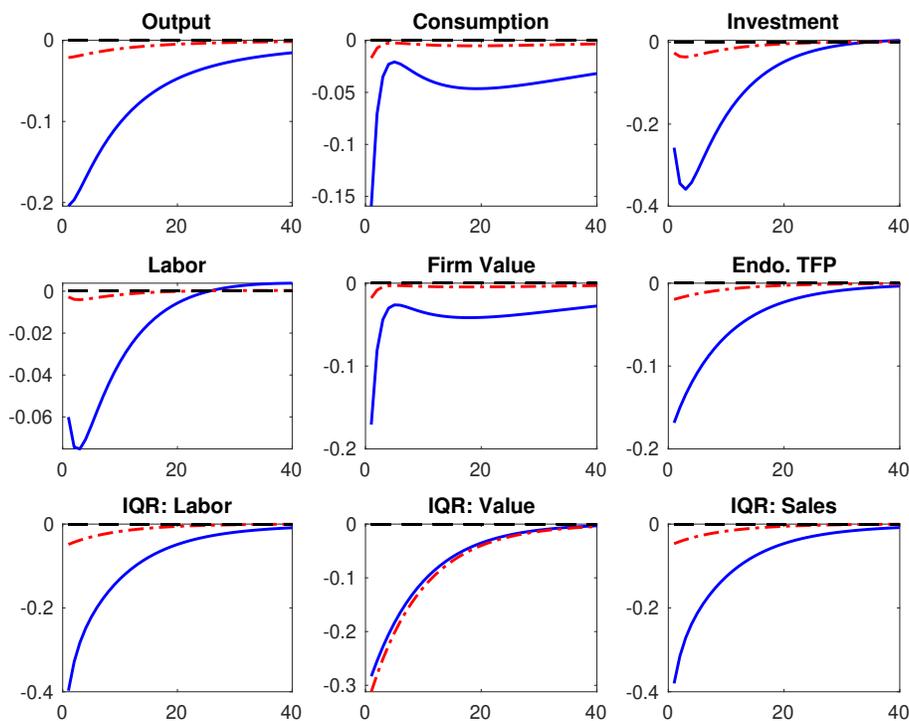
FIGURE A10. Impulse response to a turbulence shock: decreasing-return-to-scale model vs. counterfactual with quasi-fixed borrowing capacity

Note: This figure shows the impulse responses to a one-standard-deviation shock to turbulence in the decreasing-return-to-scale model (blue lines) and in the counterfactual with quasi-fixed borrowing capacity (red dash-dotted lines). The horizontal axis shows the periods (quarters) since the impact of the shock. The vertical axis shows the percent deviations of each variable from its stochastic steady-state level.

we set the subjective discount factor to $\beta = 0.96$ and the capital depreciation rate to $\delta = 0.10$. We calibrate the turbulence shock process based on our empirical measure of turbulence. In particular, the annual series of our turbulence measure (in log units) has a mean of $log(0.09)$, a standard deviation of 0.1382, and a first-order autocorrelation of 0.651. The rest of the structural parameters are identical to those in the quarterly decreasing-return-to-scale model.

Figure A11 compares the model-implied impulse responses of aggregate variables (blue solid lines) with the empirical estimates of the impulse response (black solid lines). A one-standard-deviation turbulence shock reduces aggregate output by around 0.5 percent on impact, both in the data and in the model. The shock has persistent recessionary effects on aggregate output both in the model and in the data, although the theoretical impulse responses miss the hump estimated from the data. These findings suggest that turbulence
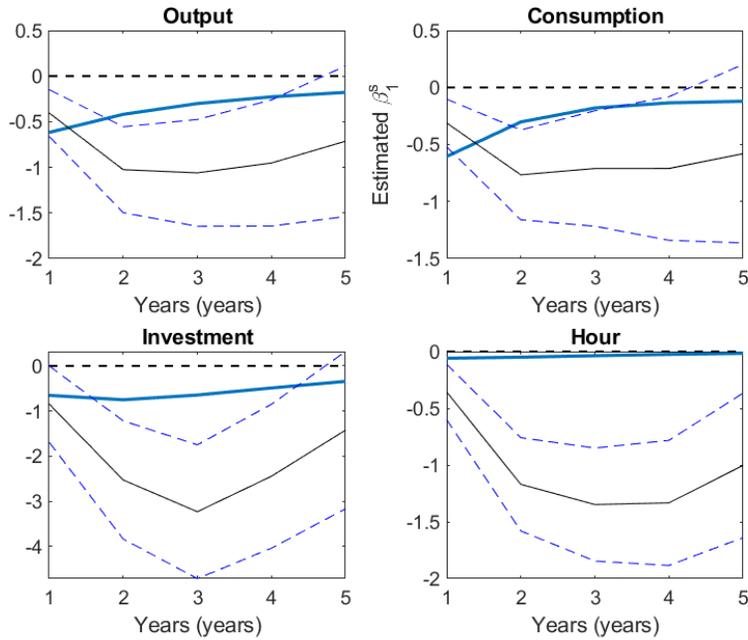
FIGURE A11. Impulse response to turbulence shock: Model vs. data (decreasing-return-to-scale)

Note: This figure shows the impulse responses of private aggregate output to a one-standard-deviation shock to turbulence in the data (black solid line) and in the calibrated annual version of the decreasing-return-to-scale model (blue solid line). The dashed lines show the 68% confidence band around the empirical estimates of the impulse responses. The horizontal axis shows the years after the impact of the shock. The vertical axis shows the percent deviations of output in the model from its steady-state level and the percentage changes in output in the data relative to its pre-shock level.

plays an important role in driving business cycles. Similar to the case of output, the model-implied responses of investment and consumption are both in line with those estimated from the data, although the calibrated model fails to generate the turbulence-driven large declines in labor hours observed in the data.